GetDP
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Obtaining GetDP

The source code and various pre-compiled versions of GetDP (for Windows, Linux and MacOS) can be downloaded from http://getdp.info.

If you use GetDP, we would appreciate that you mention it in your work. References and the latest news about GetDP are always available on http://getdp.info.
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Chapter 1: Overview

1 Overview

GetDP (a “General environment for the treatment of Discrete Problems”) is a scientific software environment for the numerical solution of integro-differential equations, open to the coupling of physical problems (electromagnetic, thermal, etc.) as well as of numerical methods (finite element method, integral methods, etc.). It can deal with such problems of various dimensions (1D, 2D or 3D) and time states (static, transient or harmonic).

The main feature of GetDP is the closeness between its internal structure (written in C), the organization of data defining discrete problems (written by the user in ASCII data files) and the symbolic mathematical expressions of these problems. Its aim is to be welcoming and of easy use for both development and application levels: it consists of a working environment in which the definition of any problem makes use of a limited number of objects, which makes the environment structured and concise. It therefore gives researchers advanced developing tools and a large freedom in adding new functionalities.

The modeling tools provided by GetDP can be tackled at various levels of complexity: this opens the software to a wide range of activities, such as research, collaboration, education, training and industrial studies.

1.1 Numerical tools as objects

An assembly of computational tools (or objects) in GetDP leads to a problem definition structure, which is a transcription of the mathematical expression of the problem, and forms a text data file: the equations describing a phenomenon, written in a mathematical form adapted to a chosen numerical method, directly constitute data for GetDP.

The resolution of a discrete problem with GetDP requires the definition, in a text data file, of the GetDP objects listed (together with their dependencies) in the following figure and table.
<table>
<thead>
<tr>
<th>Group</th>
<th>---</th>
<th>Function</th>
<th>Group</th>
<th>Constraint</th>
<th>Group, Function, (Resolution)</th>
<th>FunctionSpace</th>
<th>Group, Constraint, (Formulation), (Resolution)</th>
<th>Jacobian</th>
<th>Group</th>
<th>Integration</th>
<th>---</th>
</tr>
</thead>
</table>

The gathering of all these objects constitutes the problem definition structure, which is a copy of the formal mathematical formulation of the problem. Reading the first column of the table from top to bottom pictures the working philosophy and the linking of operations peculiar to GetDP, from group definition to results visualization. The decomposition highlighted in the figure points out the separation between the objects defining the method of resolution, which may be isolated in a “black box” (bottom) and those defining the data peculiar to a given problem (top).

The computational tools which are in the center of a problem definition structure are formulations (Formulation) and function spaces (FunctionSpace). Formulations define systems of equations that have to be built and solved, while function spaces contain all the quantities, i.e., functions, fields of vectors or covectors, known or not, involved in formulations.

Each object of a problem definition structure must be defined before being referred to by others. A linking which always respects this property is the following: it first contains the objects defining particular data of a problem, such as geometry, physical characteristics and boundary conditions (i.e., Group, Function and Constraint) followed by those defining a resolution method, such as unknowns, equations and related objects (i.e., Jacobian, Integration, FunctionSpace, Formulation, Resolution and PostProcessing). The processing cycle ends with the presentation of the results (i.e., lists of numbers in various formats), defined in PostOperation fields. This decomposition points out the possibility of building black boxes, containing objects of the second group, adapted to treatment of general classes of problems that share the same resolution methods.

### 1.2 Which problems can GetDP actually solve?

The preceding explanations may seem very (too) general. Which are the problems that GetDP can actually solve? To answer this question, here is a list of methods that we have considered and coupled until now:

**Numerical methods**
- finite element method
- boundary element method (experimental, undocumented)
- volume integral methods (experimental, undocumented)
Chapter 1: Overview

Geometrical models
  one-dimensional models (1D)
  two-dimensional models (2D), plane and axisymmetric
  three-dimensional models (3D)

Time states
  static states
  sinusoidal and harmonic states
  transient states
  eigenvalue problems

These methods have been successfully applied to build coupled physical models involving electromagnetic phenomena (magnetostatics, magnetodynamics, electrostatics, electrokinetics, electrodynamics, wave propagation, lumped electric circuits), acoustic phenomena, thermal phenomena and mechanical phenomena (elasticity, rigid body movement).

As can be guessed from the preceding list, GetDP has been initially developed in the field of computational electromagnetics, which fully uses all the offered coupling features. We believe that this does not interfere with the expected generality of the software because a particular modeling forms a problem definition structure which is totally external to the software: GetDP offers computational tools; the user freely applies them to define and solve his problem.

Nevertheless, specific numerical tools will always need to be implemented to solve specific problems in areas other than those mentioned above. If you think the general philosophy of GetDP is right for you and your problem, but you discover that GetDP lacks the tools necessary to handle it, let us know: we would love to discuss it with you. For example, at the time of this writing, many areas of GetDP would need to be improved to make GetDP as useful for computational mechanics or computational fluid dynamics as it is for computational electromagnetics... So if you have the skills and some free time, feel free to join the project: we gladly accept all code contributions!

1.3 Bug reports

Please file issues on https://gitlab.onelab.info/getdp/getdp/issues. Provide as precise a description of the problem as you can, including sample input files that produce the bug. Don’t forget to mention both the version of GetDP and the version of your operation system (see Chapter 3 [Running GetDP], page 11 to see how to get this information).

See Appendix D [Frequently asked questions], page 121, and the bug tracking system to see which problems we already know about.


2 How to read this manual

After reading Chapter 1 [Overview], page 5, which depicts the general philosophy of GetDP, you might want to skip Chapter 4 [Expressions], page 15, Chapter 5 [Objects], page 29 and Chapter 6 [Types for objects], page 43 and directly run the demo files bundled in the distribution on your computer (see Chapter 3 [Running GetDP], page 11). You should then open these examples with a text editor and compare their structure with the examples given in Chapter 7 [Short examples], page 75 and Chapter 8 [Complete examples], page 91. For each new syntax element that you fall onto, you can then go back to Chapter 4 [Expressions], page 15, Chapter 5 [Objects], page 29, and Chapter 6 [Types for objects], page 43, and find in these chapters the detailed description of the syntactic rules as well as all the available options.

Indexes for many concepts (see [Concept index], page 141) and for all the syntax elements (see [Syntax index], page 147) are available at the end of this manual.

2.1 Syntactic rules used in this document

Here are the rules we tried to follow when writing this user’s guide. Note that metasyntactic variable definitions stay valid throughout all the manual (and not only in the sections where the definitions appear). See [Metasyntactic variable index], page 145, for an index of all metasyntactic variables.

1. Keywords and literal symbols are printed like this.

2. Metasyntactic variables (i.e., text bits that are not part of the syntax, but stand for other text bits) are printed like this.

3. A colon (:) after a metasyntactic variable separates the variable from its definition.

4. Optional rules are enclosed in < > pairs.

5. Multiple choices are separated by |.

6. Three dots (…) indicate a possible repetition of the preceding rule.

7. For conciseness, the notation rule <, rule > … is replaced by rule <,…>.

8. The etc symbol replaces nonlisted rules.
3 Running GetDP

GetDP has no graphical interface\(^1\). It is a command-line driven program that reads a problem definition file once at the beginning of the processing. This problem definition file is a regular ASCII text file (see Section 1.1 [Numerical tools as objects], page 5), hence created with whatever text editor you like.

If you just type the program name at your shell prompt (without any argument), you will get a short help on how to run GetDP. All GetDP calls look like

```
getdp filename options
```

where `filename` is the ASCII file containing the problem definition, i.e., the structures this user’s guide has taught you to create. This file can include other files (see Section 4.2 [Includes], page 15), so that only one problem definition file should always be given on the command line. The input files containing the problem definition structure are usually given the ‘.pro’ extension (if so, there is no need to specify the extension on the command line). The name of this file (without the extension) is used as a basis for the creation of intermediate files during the pre-processing and the processing stages.

The `options` are a combination of the following commands (in any order):

- `pre resolution-id`
  Performs the pre-processing associated with the resolution `resolution-id`. In the pre-processing stage, GetDP creates the geometric database (from the mesh file), identifies the degrees of freedom (the unknowns) of the problem and sets up the constraints on these degrees of freedom. The pre-processing creates a file with a ‘.pre’ extension. If `resolution-id` is omitted, the list of available choices is displayed.

- `cal`
  Performs the processing. This requires that a pre-processing has been performed previously, or that a `pre` option is given on the same command line. The performed resolution is the one given as an argument to the `pre` option. In the processing stage, GetDP executes all the commands given in the Operation field of the selected Resolution object (such as matrix assemblies, system resolutions, ...).

- `pos post-operation-id ...`
  Performs the operations in the PostOperation(s) selected by the `post-operation-id`\(\text{s}\). This requires that a processing has been performed previously, or that a `cal` option is given on the same command line. If `post-operation-id` is omitted, the list of available choices is displayed.

- `msh filename`

\(^1\) If you are looking for a graphical front-end to GetDP, you may consider using Gmsh (available at \url{http://gmsh.info}). Gmsh permits to construct geometries, generate meshes, launch computations and visualize results directly from within a user-friendly graphical interface. The file formats used by Gmsh for mesh generation and post-processing are the default file formats accepted by GetDP (see Section A.1 [Input file format], page 111, and Section 6.10 [Types for PostOperation], page 68).
Reads the mesh (in .msh format) from filename (see Appendix A [File formats], page 111) rather than from the default problem file name (with the ‘.msh’ extension appended).

-msh_scaling

value

Multiplies the coordinates of all the nodes in the mesh by value.

-gmshread

filename . . .

Read gmsh data files (same as GmshRead in Resolution operations). Allows to use such datasets outside resolutions (e.g. in pre-processing).

-split

Saves processing results in separate files (one for each timestep).

-res

filename . . .

Loads processing results from file(s).

-name

string

Uses string as the default generic file name for input or output of mesh, pre-processing and processing files.

-restart

Restarts processing of a time stepping resolution interrupted before being complete.

-solve

resolution-id

Same as -pre resolution-id -cal.

-solver

filename

Specifies a solver option file (whose format varies depending on the linear algebra toolkit used).

-slepc

Uses SLEPc instead of Arpack as eigensolver.

-adapt

file

Reads adaptation constraints from file.

-order

real

 Specifies the maximum interpolation order.

-cache

Caches network computations to disk.

-bin

Selects binary format for output files.

-v2

Creates mesh-based Gmsh output files when possible.
-check

Lets you check the problem structure interactively.

-v
-verbose  integer

Sets the verbosity level. A value of 0 means that no information will be displayed during the processing.

-cpu

Reports CPU times for all operations.

-p
-progress  integer

Sets the progress update rate. This controls the refreshment rate of the counter indicating the progress of the current computation (in %).

-onelab  name <address>

Communicates with OneLab (file or server address)

-setnumber  name value

Sets constant number name to value

-setstring  name value

Sets constant string name to value

-info

Displays the version information.

-version

Displays the version number.

-help

Displays a message listing basic usage and available options.
4 Expressions

This chapter and the next two describe in a rather formal way all the commands that can be used in the ASCII text input files. If you are just beginning to use GetDP, or just want to see what GetDP is all about, you should skip this chapter and the next two for now, have a quick look at Chapter 3 [Running GetDP], page 11, and run the demo problems bundled in the distribution on your computer. You should then open the ‘.pro’ files in a text editor and compare their structure with the examples given in Chapter 7 [Short examples], page 75 and Chapter 8 [Complete examples], page 91. Once you have a general idea of how the files are organized, you might want to come back here to learn more about the specific syntax of all the objects, and all the available options.

4.1 Comments

Both C and C++ style comments are supported and can be used in the input data files to comment selected text regions:

1. the text region comprised between /* and */ pairs is ignored;
2. the rest of a line after a double slash // is ignored.

Comments cannot be used inside double quotes or inside GetDP keywords.

4.2 Includes

An input data file can be included in another input data file by placing one of the following commands (expression-char represents a file name) on a separate line, outside the GetDP objects. Any text placed after an include command on the same line is ignored.

Include expression-char
#include expression-char

See Section 4.4 [Constants], page 16, for the definition of the character expression expression-char.

4.3 Expressions definition

Expressions are the basic tool of GetDP. They cover a wide range of functional expressions, from constants to formal expressions containing functions (built-in or user-defined, depending on space and time, etc.), arguments, discrete quantities and their associated differential operators, etc. Note that ‘white space’ (spaces, tabs, new line characters) is ignored inside expressions (as well as inside all GetDP objects).

Expressions are denoted by the metasyntactic variable expression (remember the definition of the syntactic rules in Section 2.1 [Syntactic rules], page 9):

expression:
   ( expression ) | integer | real | constant-id | quantity | argument |

The following sections introduce the quantities that can appear in expressions, i.e., constant terminals (integer, real) and constant expression identifiers (constant-id, expression-cst-list), discretized fields (quantity), arguments (argument), current values (current-value), register values (register-set, register-get), operators (operator-unary, operator-binary, operator-ternary-left, operator-ternary-right) and built-in or user-defined functions (built-in-function-id, function-id). The last seven cases in this definition permit to cast an expression as real or complex, get the time derivative or evaluate an expression at an anterior time step, retrieve the interpolation order of a discretized quantity, evaluate the trace of an expression, and print the value of an expression for debugging purposes.

List of expressions are defined as:

expression-list:
expression <,...>  

4.4 Constants

The three constant types used in GetDP are integer, real and string. These types have the same meaning and syntax as in the C or C++ programming languages. Besides general expressions (expression), purely constant expressions, denoted by the metasyntactic variable expression-cst, are also used:

expression-cst:
( expression-cst ) | integer | real | constant-id | operator-unary expression-cst | expression-cst operator-binary expression-cst | expression-cst operator-ternary-left expression-cst operator-ternary-right expression-cst |
math-function-id [ < expression-cst-list > ] | 
#constant-id() | 
constant-id(expression-cst) | 
StrFind[ expression-char, expression-char ] | 
StrCmp[ expression-char, expression-char ] | 
StrLen[ expression-char ] | 
StringToName[ expression-char ] | S2N[ expression-char ] | 
GetForced[ string ] | NbrRegions[ string ] | 
GetNumber[ expression-char <, expression-cst> ]

StrFind searches the first expression-char for any occurrence of the second expression-char.
StrCmp compares the two strings (returns an integer greater than, equal to, or less than 0, according as the first string is greater than, equal to, or less than the second string).
StrLen returns the length of the string. StringToName creates a name from the provided string. Exists checks for the existence of a constant or a function. FileExists checks for the existence of a file. GroupExists checks for the existence of a group. GetForced gets the value of a constant (zero if does not exist). NbrRegions counts the numbers of elementary regions in a group. GetNumber allows to get the value of a ONELAB number variable (the optional second argument specifies the default value returned if the variable does not exist).

List of constant expressions are defined as:

expression-cst-list:
  expression-cst-list-item <,...>

with

expression-cst-list-item:
  expression-cst | 
  expression-cst : expression-cst | 
  expression-cst : expression-cst : expression-cst | 
  constant-id() | 
  constant-id ( { expression-cst-list } ) | 
  List[ constant-id ] | 
  List[ expression-cst-list-item ] | 
  List[ { expression-cst-list } ] | 
  ListAlt[ constant-id, constant-id ] | 
  ListAlt[ expression-cst-list-item, expression-cst-list-item ] | 
  LinSpace[ expression-cst, expression-cst, expression-cst ] | 
  LogSpace[ expression-cst, expression-cst, expression-cst ] | 
  - expression-cst-list-item | 
  expression-cst * expression-cst-list-item | 
  expression-cst-list-item * expression-cst | 
  expression-cst / expression-cst-list-item | 
  expression-cst-list-item / expression-cst | 
  expression-cst-list-item ^ expression-cst | 
  expression-cst-list-item + expression-cst-list-item | 
  expression-cst-list-item - expression-cst-list-item | 
  expression-cst-list-item * expression-cst-list-item | 
  expression-cst-list-item / expression-cst-list-item |
ListFromFile [ expression-char ] | 
ListFromServer [ expression-char ]

The second case in this last definition permits to create a list containing the range of numbers comprised between the two expression-cst, with a unit incrementation step. The third case also permits to create a list containing the range of numbers comprised between the two expression-cst, but with a positive or negative incrementation step equal to the third expression-cst. The fourth and fifth cases permit to reference constant identifiers (constant-ids) of lists of constants and constant identifiers of sublists of constants (see below for the definition of constant identifiers). The sixth case is a synonym for the fourth. The seventh case permits to create alternate lists: the arguments of ListAlt must be constant-ids of lists of constants of the same dimension. The result is an alternate list of these constants: first constant of argument 1, first constant of argument 2, second constant of argument 1, etc. These kinds of lists of constants are for example often used for function parameters (see Section 4.6 [Functions], page 22). The next two cases permit to create linear and logarithmic lists of numbers, respectively. The remaining cases permit to apply arithmetic operators item-wise in lists. ListFromFile reads a list of numbers from a file. ListFromServer attempts to get a list of numbers from the ONELAB variable expression-char.

Contrary to a general expression which is evaluated at runtime (thanks to an internal stack mechanism), an expression-cst is completely evaluated during the syntactic analysis of the problem (when GetDP reads the `.pro' file). The definition of such constants or lists of constants with identifiers can be made outside or inside any GetDP object. The syntax for the definition of constants is:

affectation:
DefineConstant [ constant-id < = expression-cst > <,...> ]; |
DefineConstant [ constant-id = { expression-cst , onelab-options } <,...> ]; |
DefineConstant [ string-id < = string-def > <,...> ]; |
DefineConstant [ string-id = { string-def , onelab-options } <,...> ]; |
custom-id <()> = constant-def; |
custom-id = DefineNumber[ constant-def, onelab-options ];
string-id <()> = string-def; |
string-id = DefineString[ string-def, onelab-options ]; |
Printf [ "string" ] < > | >> string-def >; |
Printf [ "string", expression-cst-list ] < > | >> string-def >; |
Read [ constant-id ]; |
Read [ constant-id , expression-cst ]; |
UndefineConstant | Delete [ constant-id ];
UndefineFunction [ constant-id ];
SetNumber[ string , expression-cst ];
SetString[ string , string-def ];

with
constant-id:
string |

string ( expression-cst-list ) |
string ~ { expression-cst } <,...>
expression-cst-list-item | 
{ expression-cst-list }

string-id:  
string | 
string ~ { expression-cst } <,...>

string-def:  
"string" | 
StrCat[ expression-char <,...> ] | 
Str[ expression-char <,...> ]

Notes:
1. Five constants are predefined in GetDP: Pi (3.1415926535897932), 0D (0), 1D (1), 2D (2) and 3D (3).
2. When ~{expression-cst} is appended to a string string, the result is a new string formed by the concatenation of string, _ (an underscore) and the value of the expression-cst. This is most useful in loops (see Section 4.11 [Macros loops and conditionals], page 27), where it permits to define unique strings automatically. For example,
   
   For i In {1:3}
      x~{i} = i;
   EndFor

   is the same as
   
   x_1 = 1;
   x_2 = 2;
   x_3 = 3;

3. The assignment in DefineConstant (zero if no expression-cst is given) is performed only if constant-id has not yet been defined. This kind of explicit default definition mechanism is most useful in general problem definition structures making use of a large number of generic constants, functions or groups. When exploiting only a part of a complex problem definition structure, the default definition mechanism allows to define the quantities of interest only, the others being assigned a default value (that will not be used during the processing but that avoids the error messages produced when references to undefined quantities are made).

When onelab-options are provided, the parameter is exchanged with the ONELAB server. See https://gitlab.onelab.info/doc/tutorials.wikis/ONELAB-syntax-for-Gmsh-and-GetDP for more information.

4. DefineNumber and DefineString allow to define a ONELAB parameter. In this case the affectation always takes place. SetNumber and SetString allow the direct setting of ONELAB parameters without defining local variables.

See Section 7.1 [Constant expression examples], page 75, as well as Section 7.3 [Function examples], page 75, for some examples.

Character expressions are defined as follows:

expression-char:
  "string" |
string-id | 
StrCat[ expression-char <,...> ] | 
Str[ expression-char <,...> ] | 
StrChoice[ expression, expression-char, expression-char ] | 
StrSub[ expression-char, expression, expression ] | 
StrSub[ expression-char, expression ] | 
UpperCase [ expression-char ] | 
Sprintf [ expression-char ] | 
Sprintf[ expression-char, expression-cst-list ] | 
NameToString ( string ) | N2S ( string ) | 
GetString[ expression-char <, expression-char,> ] | 
Date | CurrentDirectory | CurrentDir | 
AbsolutePath [ expression-char ] | 
DirName [ expression-char ] | 
OnelabAction

StrCat and Str permit to concatenate character expressions (Str adds a newline character after each string except the last) when creating a string. Str is also used to create string lists (when string-id is followed by ()). StrChoice returns the first or second expression-char depending on the value of expression. StrSub returns the portion of the string that starts at the character position given by the first expression and spans the number of characters given by the second expression or until the end of the string (whichever comes first; or always if the second expression is not provided). UpperCase converts the expression-char to upper case. Sprintf is equivalent to the sprintf C function (where expression-char is a format string that can contain floating point formatting characters: %e, %g, etc.). NameToString converts a variable name into a string. GetString allows to get the value of a ONELAB string variable (the optional second argument specifies the default value returned if the variable does not exist.) Date permits to access the current date. CurrentDirectory and CurrentDir return the directory of the .pro file. AbsolutePath returns the absolute path of a file. DirName returns the directory of a file. OnelabAction returns the current ONELAB action (e.g. check or compute).

List of character expressions are defined as:

expression-char-list:
expression-char <,...>

4.5 Operators

4.5.1 Operator types

The operators in GetDP are similar to the corresponding operators in the C or C++ programming languages.

operator-unary:
- Unary minus.
! Logical not.

operator-binary:
\[ ^\text{Exponentiation. The evaluation of the both arguments must result in a scalar value.} \]
\[ \ast \text{Multiplication or scalar product, depending on the type of the arguments.} \]
\[ \backslash \text{Cross product. The evaluation of both arguments must result in vectors.} \]
\[ / \text{Division.} \]
\[ \% \text{Modulo. The evaluation of the second argument must result in a scalar value.} \]
\[ + \text{Addition.} \]
\[ - \text{Subtraction.} \]
\[ == \text{Equality.} \]
\[ != \text{Inequality.} \]
\[ \text{Greater. The evaluation of both arguments must result in scalar values.} \]
\[ \geq \text{Greater or equality. The evaluation of both arguments must result in scalar values.} \]
\[ < \text{Less. The evaluation of both arguments must result in scalar values.} \]
\[ \leq \text{Less or equality. The evaluation of both arguments must result in scalar values.} \]
\[ \&\& \text{Logical ‘and’. The evaluation of both arguments must result in scalar values.} \]
\[ || \text{Logical ‘or’. The evaluation of both arguments must result in floating point values. Warning: the logical ‘or’ always (unlike in C or C++) implies the evaluation of both arguments. That is, the second operand of || is evaluated even if the first one is true.} \]
\[ \& \text{Binary ‘and’.} \]
\[ | \text{Binary ‘or’.} \]
\[ \gg \text{Bitwise right-shift operator. Shifts the bits of the first argument to the right by the number of bits specified by the second argument.} \]
\[ \ll \text{Bitwise left-shift operator. Shifts the bits of the first argument to the left by the number of bits specified by the second argument.} \]

\[ \text{operator-ternary-left:} \]
\[ ? \]
\[ \text{operator-ternary-right:} \]
\[ : \text{The only ternary operator, formed by operator-ternary-left and operator-ternary-right is defined as in the C or C++ programming languages. The ternary operator first evaluates its first argument (the expression-cst located before the ?), which must result in a scalar value. If it is true (non-zero) the second argument (located between ? and :) is evaluated and returned; otherwise the third argument (located after :) is evaluated and returned.} \]
4.5.2 Evaluation order

The evaluation priorities are summarized below (from stronger to weaker, i.e., ~ has the highest evaluation priority). Parentheses () may be used anywhere to change the order of evaluation.

- 
- (unary), !
| &
/\
*, /, %
+, -
<, >, <=, >=, <<, >>
!=, ==
&&, ||
?

4.6 Functions

Two types of functions coexist in GetDP: user-defined functions (function-id, see Section 5.2 [Function], page 30) and built-in functions (built-in-function-id, defined in this section).

Both types of functions are always followed by a pair of brackets [] that can possibly contain arguments (see Section 4.8 [Arguments], page 24). This makes it simple to distinguish a function-id or a built-in-function-id from a constant-id. As shown below, built-in functions might also have parameters, given between braces {}, and which are completely evaluated during the analysis of the syntax (since they are of expression-cst-list type):

    built-in-function-id [ < expression-list > ] < { expression-cst-list } >

with

    built-in-function-id:
        math-function-id |
        extended-math-function-id |
        green-function-id |
        type-function-id |
        coord-function-id |
        misc-function-id

Notes:

1. All possible values for built-in-function-id are listed in Section 6.2 [Types for Function], page 44.

2. Classical mathematical functions (see Section 6.2.1 [Math functions], page 44) are the only functions allowed in a constant definition (see the definition of expression-cst in Section 4.4 [Constants], page 16).
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4.7 Current values

Current values return the current floating point value of an internal GetDP variable:

$\text{Time}$  Value of the current time. This value is set to zero for non time dependent analyses.

$\text{DTime}$  Value of the current time increment used in a time stepping algorithm.

$\text{Theta}$  Current theta value in a theta time stepping algorithm.

$\text{TimeStep}$  Number of the current time step in a time stepping algorithm.

$\text{Breakpoint}$  In case of a breakpoint hit in TimeLoopAdaptive it is the number of the current breakpoint. In the other case when $\text{Time}$ corresponds not to a breakpoint the value is -1.

$\text{Iteration}, \text{NLIteration}$  Current iteration in a nonlinear loop.

$\text{Residual}, \text{NLResidual}$  Current residual in a nonlinear loop.

$\text{EigenvalueReal}$  Real part of the current eigenvalue.

$\text{EigenvalueImag}$  Imaginary part of the current eigenvalue.

$\text{X}, \text{XS}$  Value of the current (destination or source) X-coordinate.

$\text{Y}, \text{YS}$  Value of the current (destination or source) Y-coordinate.

$\text{Z}, \text{ZS}$  Value of the current (destination or source) Z-coordinate.

$\text{A}, \text{B}, \text{C}$  Value of the current parametric coordinates used in the parametric OnGrid PostOperation (see Section 6.10 [Types for PostOperation], page 68).

$\text{QuadraturePointIndex}$  Index of the current quadrature point.

$\text{KSPIteration}$  Current iteration in a Krylov subspace solver.

$\text{KSPResidual}$  Current residual in a Krylov subspace solver.

$\text{KSPIterations}$  Total number of iterations of Krylov subspace solver.

$\text{KSPSystemSize}$  System size of Krylov subspace solver.

Note:
1. The current X, Y and Z coordinates refer to the ‘physical world’ coordinates, i.e.,
coordinates in which the mesh is expressed.

Current values are “read-only”. User-defined run-time variables, which share the same
syntax but whose value can be changed in an expression, are defined in Section 4.9 [Run-
time variables and registers], page 24.

4.8 Arguments

Function arguments can be used in expressions and have the following syntax (integer
indicates the position of the argument in the expression-list of the function, starting from
1):

\[ \text{argument:} \]
\[ $ \text{integer} \]

See Section 5.2 [Function], page 30, and Section 7.3 [Function examples], page 75, for more
details.

4.9 Run-time variables and registers

Constant expressions \( (\text{expression-cst}s) \) are evaluated only once during the analysis of the
problem definition structure, cf. Section 4.4 [Constants], page 16. While this is perfectly
fine in most situations, sometimes it is necessary to store and modify variables at run-time.
For example, an iteration in a Resolution could depend on values computed at run-time.
Also, to speed-up the evaluation of expressions (which are evaluated at runtime through
GetDP’s internal stack mechanism), it can be useful to save some results in a temporary
variable, at run-time, in order to reuse them later on.

Two mechanisms exit to handle such cases: run-time variables (which follow the same
syntax as Section 4.7 [Current values], page 23), and registers.

Run-time variables have the following syntax:

\[ \text{variable-set:} \]
\[ $\text{variable-id} = \text{expression} \]

\[ \text{variable-get:} \]
\[ $\text{variable-id} \]

\[ \text{variable-id:} \]
\[ \text{string |} \]
\[ \text{string ~ \{ expression-cst \} <,...>} \]

Thus, run-time variables can simply be defined anywhere in an expression and be reused
later on. Current values can be seen as special cases of run-time variables, which are read-
only.

Registers have the following syntax:

\[ \text{register-set:} \]
\[ \text{expression#expression-cst} \]

\[ \text{register-get:} \]
#expression-cst

Thus, to store any expression in the register 5, one should add \#5 directly after the expression. To reuse the value stored in this register, one simply uses \#5 instead of the expression it should replace.

See Section 7.3 [Function examples], page 75, for an example.

## 4.10 Fields

A discretized quantity (defined in a function space, cf. Section 5.4 [FunctionSpace], page 32) is represented between braces \{\}, and can only appear in well-defined expressions in Formulation (see Section 5.7 [Formulation], page 36) and PostProcessing (see Section 5.9 [PostProcessing], page 39) objects:

\[
\text{quantity:} \\
\langle \text{quantity-dof} \rangle \{ \langle \text{quantity-operator} \rangle \text{quantity-id} \} \\
\{ \langle \text{quantity-operator} \rangle \text{quantity-id} \} [ \text{expression-cst-list} ]
\]

with

\[
\text{quantity-id:} \\
\text{string} | \\
\text{string} ~ \{ \text{expression-cst} \}
\]

and

\[
\text{quantity-dof:} \\
\text{Dof} \quad \text{Defines a vector of discrete quantities (vector of Degrees of freedom), to be used only in Equation terms of formulations to define (elementary) matrices. Roughly said, the Dof symbol in front of a discrete quantity indicates that this quantity is an unknown quantity, and should therefore not be considered as already computed. An Equation term must be linear with respect to the Dof. Thus, for example, a nonlinear term like} \\
\text{Integral} \{ \langle \text{quantity-operator} \rangle \text{quantity-id} \} \langle \text{quantity-operator} \rangle \text{quantity-id} \langle \text{quantity-operator} \rangle \text{quantity-id} \} \{ \text{expression-cst-list} \}
\]

must first be linearized; and while

\[
\text{Integral} \{ \langle \text{quantity-operator} \rangle \text{quantity-id} \} \langle \text{quantity-operator} \rangle \text{quantity-id} \langle \text{quantity-operator} \rangle \text{quantity-id} \} \{ \text{expression-cst-list} \}
\]

is valid, the following, which is affine but not linear, is not:

\[
\text{Integral} \{ \langle \text{quantity-operator} \rangle \text{quantity-id} \} \langle \text{quantity-operator} \rangle \text{quantity-id} \langle \text{quantity-operator} \rangle \text{quantity-id} \} \{ \text{expression-cst-list} \}
\]

GetDP supports two linearization techniques. The first is functional iteration (or Picard method), where one simply plugs the value obtained at the previous iteration into the nonlinear equation (the previous value is known, and is accessed e.g. with \{T\} instead \text{Dof(T)}). The second is the Newton-Raphson iteration, where the Jacobian is specified with a \text{JacNL} equation term.

\[
\text{BF} \quad \text{Indicates that only a basis function will be used (only valid with basis functions associated with regions).}
\]

\[
\text{quantity-operator:} \\
d \quad \text{Exterior derivative (d): applied to a p-form, gives a (p+1)-form.}
\]
Grad  Gradient: applied to a scalar field, gives a vector.

Curl  Curl: applied to a vector field, gives a vector.

Div  Divergence (div): applied to a vector field, gives a scalar.

D1  Applies the operator specified in the first argument of \texttt{dFunction \{basis-function-type, basis-function-type\}} (see Section 5.4 [FunctionSpace], page 32). This is currently only used for nodal-interpolated vector fields (interpolated with BF_Node_X, BF_Node_Y, BF_Node_Z).

When the first \textit{basis-function-type} in \texttt{dFunction} is set to BF_NodeX_D1 for component X, BF_NodeY_D1 for component Y and BF_NodeZ_D1 for component Z, then D1 applied to a vector \([u_x, u_y, u_z] \) gives:

\[
\begin{bmatrix}
\frac{\partial u_x}{\partial x}, \frac{\partial u_y}{\partial y}, \frac{\partial u_z}{\partial z}
\end{bmatrix}
\]

Note that in this case specifying explicitly \texttt{dFunction} is not necessary, as BF_NodeX_D1, BF_NodeY_D1 and BF_NodeZ_D1 are assigned by default as the “D1 derivatives” of BF_NodeX, BF_NodeY and BF_NodeZ. This also holds for BF_GroupOfNodes_X, BF_GroupOfNodes_Y and BF_GroupOfNodes_Z.

When the first \textit{basis-function-type} in \texttt{dFunction} is set to BF_NodeX_D12 for component X and BF_NodeY_D12 for component Y, then D1 applied to a vector \([u_x, u_y, u_z] \) gives:

\[
\begin{bmatrix}
\frac{\partial u_y}{\partial x} + \frac{\partial u_x}{\partial y}, \frac{\partial u_z}{\partial y}, \frac{\partial u_y}{\partial z} + \frac{\partial u_z}{\partial x}
\end{bmatrix}
\]

D2  Applies the operator specified in the second argument of \texttt{dFunction \{basis-function-type, basis-function-type\}} (see Section 5.4 [FunctionSpace], page 32). This is currently only used for nodal-interpolated vector fields (interpolated with BF_Node_X, BF_Node_Y, BF_Node_Z).

More specifically, when the second \textit{basis-function-type} is to BF_NodeX_D2 for component X, BF_NodeY_D2 for component Y and BF_NodeZ_D2 for component Z, then D2 applied to a vector \([u_x, u_y, u_z] \) gives:

\[
\begin{bmatrix}
\frac{\partial u_y}{\partial x} + \frac{\partial u_x}{\partial y} + \frac{\partial u_z}{\partial y}, \frac{\partial u_y}{\partial z} + \frac{\partial u_z}{\partial x} + \frac{\partial u_x}{\partial z}
\end{bmatrix}
\]

Note that in this case specifying explicitly \texttt{dFunction} is not necessary, as BF_NodeX_D2, BF_NodeY_D2 and BF_NodeZ_D2 are assigned by default as the “D2 derivatives” of BF_NodeX, BF_NodeY and BF_NodeZ. This also holds for BF_GroupOfNodes_X, BF_GroupOfNodes_Y and BF_GroupOfNodes_Z.

Notes:

1. While the operators Grad, Curl and Div can be applied to 0, 1 and 2-forms respectively, the exterior derivative operator \(d\) is usually preferred with such fields.

2. The second case permits to evaluate a discretized quantity at a certain position X, Y, Z (when \textit{expression-cst-list} contains three items) or at a specific time, \(N\) time steps ago (when \textit{expression-cst-list} contains a single item).
4.11 Macros, loops and conditionals

Macros are defined as follows:

**Macro string | expression-char**

Begins the declaration of a user-defined file macro named *string*. The body of the macro starts on the line after `Macro string`, and can contain any GetDP command.

**Return**

Ends the body of the current user-defined file macro. Macro declarations cannot be imbricated, and must be made outside any GetDP object.

**Macro ( expression-char , expression-char ) ;**

Begins the declaration of a user-defined string macro. The body of the macro is given explicitly as the second argument.

Macros, loops and conditionals can be used in any of the following objects: Group, Function, Constraint (as well as in a contraint-case), FunctionSpace, Formulation (as well as in the quantity and equation definitions), Resolution (as well as resolution-term, system definition and operations), PostProcessing (in the definition of the PostQuantities) and PostOperation (as well as in the operation list).

**loop:**

**Call string | expression-char ;**

Executes the body of a (previously defined) macro named *string*.

**For ( expression-cst : expression-cst )**

Iterates from the value of the first *expression-cst* to the value of the second *expression-cst*, with a unit incrementation step. At each iteration, the commands comprised between `For ( expression-cst : expression-cst )` and the matching `EndFor` are executed.

**For ( expression-cst : expression-cst : expression-cst )**

Iterates from the value of the first *expression-cst* to the value of the second *expression-cst*, with a positive or negative incrementation step equal to the third *expression-cst*. At each iteration, the commands comprised between `For ( expression-cst : expression-cst : expression-cst )` and the matching `EndFor` are executed.

**For string In { expression-cst : expression-cst }**

Iterates from the value of the first *expression-cst* to the value of the second *expression-cst*, with a unit incrementation step. At each iteration, the value of the iterate is affected to an expression named *string*, and the commands comprised between `For string In { expression-cst : expression-cst }` and the matching `EndFor` are executed.

**For string In { expression-cst : expression-cst : expression-cst }**

Iterates from the value of the first *expression-cst* to the value of the second *expression-cst*, with a positive or negative incrementation step equal to the third *expression-cst*. At each iteration, the value of the iterate is affected to an expression named *string*, and the commands comprised between `For string In { expression-cst : expression-cst : expression-cst }` and the matching `EndFor` are executed.
EndFor  Ends a matching For command.

If ( expression-cst )
   The body enclosed between ‘If ( expression-cst )’ and the matching
   ElseIf, Else or EndIf, is evaluated if expression-cst is non-zero.

ElseIf ( expression-cst )
   The body enclosed between ‘ElseIf ( expression-cst )’ and the next matching
   ElseIf, Else or EndIf, is evaluated if expression-cst is non-zero and none of
   the expression-cst of the previous matching codes If and ElseIf were non-zero.

Else  The body enclosed between Else and the matching EndIf is evaluated if none of
      the expression-cst of the previous matching codes If and ElseIf were non-zero.

EndIf  Ends a matching If command.

LevelTest
   Variable equal to the level of imbrication of a body in an If-EndIf test.

Parse [ expression-char ];
   Parse the given string.
5 Objects

This chapter presents the formal definition of the ten GetDP objects mentioned in Chapter 1 [Overview], page 5. To be concise, all the possible parameters for these objects are not given here (cf. the etc syntactic rule defined in Section 2.1 [Syntactic rules], page 9). Please refer to Chapter 6 [Types for objects], page 43, for the list of all available options.

5.1 Group: defining topological entities

Meshes (grids) constitute the input data of GetDP. All that is needed by GetDP as a mesh is a file containing a list of nodes (with their coordinates) and a list of geometrical elements with, for each one, a number characterizing its geometrical type (i.e., line, triangle, quadrangle, tetrahedron, hexahedron, prism, etc.), a number characterizing the physical region to which it belongs and the list of its nodes. This minimal input set should be easy to extract from most of the classical mesh file formats (see Section A.1 [Input file format], page 111, for a complete description of the mesh file format read by GetDP).

Groups of geometrical entities of various types can be considered and are used in many objects. There are region groups, of which the entities are regions, and function groups, with nodes, edges, facets, volumes, groups of nodes, edges of tree, facets of tree, ... of regions.

Amongst region groups, elementary and global groups can be distinguished: elementary groups are relative to single regions (e.g., physical regions in which piecewise defined functions or constraints can be defined) while global groups are relative to sets of regions for which given treatments have to be performed (e.g., domain of integration, support of a function space, etc.).

Groups of function type contain lists of entities built on some region groups (e.g., nodes for nodal elements, edges for edge elements, edges of tree for gauge conditions, groups of nodes for floating potentials, elements on one side of a surface for cuts, etc.).

A definition of initially empty groups can be obtained thanks to a DefineGroup command, so that their identifiers exist and can be referred to in other objects, even if these groups are not explicitly defined. This procedure is similar to the DefineConstant procedure introduced for constants in Section 4.4 [Constants], page 16.

The syntax for the definition of groups is:

```
Group {
  < DefineGroup [ group-id <{integer}> <,...> ]; > ...
  < group-id = group-def; > ...
  < group-id += group-def; > ...
  < group-id -= group-def; > ...
  < affectation > ...
  < loop > ...
}
```

with

- `group-id`: string |
- `string " { expression-cst }`
group-def:
  group-type [ group-list <, group-sub-type group-list > ] |
  group-id {<integer>}> |
  #group-list

group-type:
  Region | Global | NodesOf | EdgesOf | etc

group-list:
  All | group-list-item | { group-list-item <,...> }

group-list-item:
  integer |
  integer : integer |
  integer : integer : integer |
  group-id {<integer>}

group-sub-type:
  Not | StartingOn | OnPositiveSideOf | etc

Notes:

1. integer as a group-list-item is the only interface with the mesh; with each element is associated a region number, being this integer, and a geometrical type (see Section A.1 [Input file format], page 111). Ranges of integers can be specified in the same way as ranges of constant expressions in an expression-cst-list-item (see Section 4.4 [Constants], page 16). For example, i:j replaces the list of consecutive integers i, i+1, ..., j-1, j.

2. Array of groups: DefineGroup[group-id{i}] defines the empty groups group-id{i}, i=1, ..., n. Such a definition is optional, i.e., each group-id{i} can be separately defined, in any order.

3. #group-list is an abbreviation of Region[group-list].

See Section 6.1 [Types for Group], page 43, for the complete list of options and Section 7.2 [Group examples], page 75, for some examples.

5.2 Function: defining global and piecewise expressions

A user-defined function can be global in space or piecewise defined in region groups. A physical characteristic is an example of a piecewise defined function (e.g., magnetic permeability, electric conductivity, etc.) and can be simply a constant, for linear materials, or a function of one or several arguments for nonlinear materials. Such functions can of course depend on space coordinates or time, which can be needed to express complex constraints.

A definition of initially empty functions can be made thanks to the DefineFunction command so that their identifiers exist and can be referred to (but cannot be used) in other objects. The syntax for the definition of functions is:

Function {
  < DefineFunction [ function-id <,...> ]; > ...
<function-id [ <group-def <, group-def > ] = expression; > ...
< affectation > ...
< loop > ...
}

with

function-id:
string

Note:
1. The first optional group-def in brackets must be of Region type, and indicates on which region the (piecewise) function is defined. The second optional group-def in brackets, also of Region type, defines an association with a second region for mutual contributions. A default piecewise function can be defined with All for group-def, for all the other non-defined regions. Warning: it is incorrect to write \( f[\text{reg1}]=1; \ g[\text{reg2}]=f[]+1; \) since the domains of definition of \( f[] \) and \( g[] \) don’t match.

2. One can also define initially empty functions inline by replacing the expression with ***.

See Section 6.2 [Types for Function], page 44, for the complete list of built-in functions and Section 7.3 [Function examples], page 75, for some examples.

5.3 Constraint: specifying constraints on function spaces and formulations

Constraints can be referred to in FunctionSpace objects to be used for boundary conditions, to impose global quantities or to initialize quantities. These constraints can be expressed with functions or be imposed by the pre-resolution of another discrete problem. Other constraints can also be defined, e.g., constraints of network type for the definition of circuit connections, to be used in Formulation objects.

The syntax for the definition of constraints is:

Constraint {
  { < Append < expression-cst >; >
    Name constraint-id; Type constraint-type;
    Case {
      { Region group-def; < Type constraint-type; >
        < SubRegion group-def; > < TimeFunction expression; >
        < RegionRef group-def; > < SubRegionRef group-def; >
        < Coefficient expression; > < Function expression; >
        < Filter expression; >
        constraint-val; } ...
        < loop > ...
      }
      | Case constraint-case-id {
        { Region group-def; < Type constraint-type; >
          constraint-case-val; } ...
        < loop > ...
      }
    ...
  }
} ...
...<affectation>...
<loop>...

} with

constraint-id:
case-id:
string |
string " { expression-cst }

type:
Assign | Init | Network | Link | etc

case-val:
Value expression | NameOfResolution resolution-id | etc

case-val:
Branch { integer, integer } | etc

Notes:
1. The optional Append < expression-cst > (when the optional level expression-cst is strictly positive) permits to append an existing Constraint of the same Name with additional Cases.
2. The constraint type constraint-type defined outside the Case fields is applied to all the cases of the constraint, unless other types are explicitly given in these cases. The default type is Assign.
3. The region type Region group-def will be the main group-list argument of the group-def to be built for the constraints of FunctionSpaces. The optional region type SubRegion group-def will be the argument of the associated group-sub-type.
4. expression in Value of case-val cannot be time dependent ($Time$) because it is evaluated only once during the pre-processing (for efficiency reasons). Time dependences must be defined in TimeFunction expression.

See Section 6.3 [Types for Constraint], page 54, for the complete list of options and Section 7.4 [Constraint examples], page 77, for some examples.

5.4 FunctionSpace: building function spaces

A FunctionSpace is characterized by the type of its interpolated fields, one or several basis functions and optional constraints (in space and time). Subspaces of a function space can be defined (e.g., for the use with hierarchical elements), as well as direct associations of global quantities (e.g., floating potential, electric charge, current, voltage, magnetomotive force, etc.).

A key point is that basis functions are defined by any number of subsets of functions, being added. Each subset is characterized by associated built-in functions for evaluation, a support of definition and a set of associated supporting geometrical entities (e.g., nodes, edges, facets, volumes, groups of nodes, edges incident to a node, etc.). The freedom in
defining various kinds of basis functions associated with different geometrical entities to interpolate a field permits to build made-to-measure function spaces adapted to a wide variety of field approximations (see Section 7.5 [FunctionSpace examples], page 78).

The syntax for the definition of function spaces is:

```
FunctionSpace {
    { < Append < expression-cst >; >
        Name function-space-id;
        Type function-space-type;
        BasisFunction {
            { Name basis-function-id; NameOfCoef coef-id;
                Function basis-function-type
                < { Quantity quantity-id;
                    Formulation formulation-id { expression-cst };}
                Group group-def;
                Resolution resolution-id { expression-cst } >;
                < dFunction { basis-function-type, basis-function-type } ; >
                Support group-def; Entity group-def; } ... }
    }
    < SubSpace {
        { < Append < expression-cst >; >
            Name sub-space-id;
            NameOfBasisFunction basis-function-list; } ... }
    }
    < GlobalQuantity {
        { Name global-quantity-id; Type global-quantity-type;
            NameOfCoef coef-id; } ... }
    }
    < Constraint {
        { NameOfCoef coef-id;
            EntityType Auto | group-type; < EntitySubType group-sub-type; >
            NameOfConstraint constraint-id <{}>; } ... }
    } ...
    < affectation > ...
    < loop > ...
}
```

with

- `function-space-id`:
- `formulation-id`:
- `resolution-id`:
  - `string` |
  - `string` ~ `{ expression-cst }

- `basis-function-id`:
- `coef-id`:
- `sub-space-id`:
**global-quantity-id**:  
string

**function-space-type**:  
Scalar | Vector | Form0 | Form1 | etc

**basis-function-type**:  
BF_Node | BF_Edge | etc

**basis-function-list**:  

**global-quantity-type**:  
AliasOf | AssociatedWith

Notes:

1. The optional `Append < expression-cst >` (when the optional level `expression-cst` is strictly positive; its omission fixes it to a top value) permits to append an existing `FunctionSpace` of the same `Name` with additional `BasisFunctions`, `SubSpaces`, `GlobalQuantity`'s and `Constraints`, or an existing `SubSpace` of the same `Name` with additional `NameOfBasisFunction`'s. If the `Append FunctionSpace` level is 2, the `Append SubSpace` level is automatically 1 if omitted.

2. When the definition region of a function type group used as an `Entity` of a `BasisFunction` is the same as that of the associated `Support`, it is replaced by `All` for more efficient treatments during the computation process (this prevents the construction and the analysis of a list of geometrical entities).

3. The same `Name` for several `BasisFunction` fields permits to define piecewise basis functions; separate `NameOfCoef` must be defined for those fields.

4. A constraint is associated with geometrical entities defined by an automatically created `Group` of type `group-type` (`Auto` automatically fixes it as the `Entity group-def` type of the related `BasisFunction`), using the `Region` defined in a `Constraint` object as its main argument, and the optional `SubRegion` in the same object as a `group-sub-type` argument.

5. A global basis function (`BF_Global` or `BF_dGlobal`) needs parameters, i.e., it is given by the quantity (`quantity-id`) pre-computed from multiresolutions performed on multi-formulations.

6. Explicit derivatives of the basis functions can be specified using `dFunction { basis-function-type , basis-function-type }`. These derivates can be accessed using the special `D1` and `D2` operators (see Section 4.10 [Fields], page 25).

See Section 6.4 [Types for FunctionSpace], page 55, for the complete list of options and Section 7.5 [FunctionSpace examples], page 78, for some examples.

**5.5 Jacobian: defining jacobian methods**

Jacobian methods can be referred to in `Formulation` and `PostProcessing` objects to be used in the computation of integral terms and for changes of coordinates. They are based on
Group objects and define the geometrical transformations applied to the reference elements (i.e., lines, triangles, quadrangles, tetrahedra, prisms, hexahedra, etc.). Besides the classical lineic, surfacic and volume Jacobians, the **Jacobian** object allows the construction of various transformation methods (e.g., infinite transformations for unbounded domains) thanks to dedicated jacobian methods.

The syntax for the definition of Jacobian methods is:

```plaintext
Jacobian {
    { < Append < expression-cst >; >
        Name jacobian-id;
        Case {
            { Region group-def | All;
                Jacobian jacobian-type < { expression-cst-list } >; }
        }
    } ...
}
```

with

- **jacobian-id**: string
- **jacobian-type**: Vol | Sur | VolAxi | etc

Note:
1. The optional **Append < expression-cst >** (when the optional level **expression-cst** is strictly positive) permits to append an existing **Jacobian** of the same **Name** with additional Cases.
2. The default case of a **Jacobian** object is defined by **Region All** and must follow all the other cases.

See Section 6.5 [Types for Jacobian], page 56, for the complete list of options and Section 7.6 [Jacobian examples], page 82, for some examples.

### 5.6 Integration: defining integration methods

Various numerical or analytical integration methods can be referred to in **Formulation** and **PostProcessing** objects to be used in the computation of integral terms, each with a set of particular options (number of integration points for quadrature methods—which can be linked to an error criterion for adaptative methods, definition of transformations for singular integrations, etc.). Moreover, a choice can be made between several integration methods according to a criterion (e.g., on the proximity between the source and computation points in integral formulations).

The syntax for the definition of integration methods is:

```plaintext
Integration {
    { < Append < expression-cst >; >
        Name integration-id; < Criterion expression; >
        Case {
            < { Type integration-type;
```
Case {
    { GeoElement element-type; NumberOfPoints expression-cst } ...
}
} ... >
< { Type Analytic; } ... >
}
... 
}

with

integration-id:
    string

integration-type:
    Gauss | etc

element-type:
    Line | Triangle | Tetrahedron etc

Note:
1. The optional Append < expression-cst > (when the optional level expression-cst is strictly positive) permits to append an existing Integration of the same Name with additional Cases.

See Section 6.6 [Types for Integration], page 58, for the complete list of options and Section 7.7 [Integration examples], page 83, for some examples.

5.7 Formulation: building equations

The Formulation tool permits to deal with volume, surface and line integrals with many kinds of densities to integrate, written in a form that is similar to their symbolic expressions (it uses the same expression syntax as elsewhere in GetDP), which therefore permits to directly take into account various kinds of elementary matrices (e.g., with scalar or cross products, anisotropies, nonlinearities, time derivatives, various test functions, etc.). In case nonlinear physical characteristics are considered, arguments are used for associated functions. In that way, many formulations can be directly written in the data file, as they are written symbolically. Fields involved in each formulation are declared as belonging to beforehand defined function spaces. The uncoupling between formulations and function spaces allows to maintain a generality in both their definitions.

A Formulation is characterized by its type, the involved quantities (of local, global or integral type) and a list of equation terms. Global equations can also be considered, e.g., for the coupling with network relations.

The syntax for the definition of formulations is:

Formulation {
    { < Append < expression-cst >; >
        Name formulation-id; Type formulation-type;
        Quantity {
            { Name quantity-id; Type quantity-type; 

    ... 
}
}
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NameOfSpace function-space-id <{}>
   < [ sub-space-id | global-quantity-id ] >;
   < Symmetry expression-cst; >
   < [ expression ]; In group-def;
      Jacobian jacobian-id; Integration integration-id; >
   < IndexOfSystem integer; > } ...
}
Equation {
   < local-term-type 
      { < term-op-type > [ expression, expression ];
         In group-def; Jacobian jacobian-id; Integration integration-id; } > ...
   < GlobalTerm
      { < term-op-type > [ expression, expression ];
         In group-def; < SubType equation-term-sub-type; > } > ...
   < GlobalEquation
      { Type Network; NameOfConstraint constraint-id;
         { Node expression; Loop expression; Equation expression;
            In group-def; } ... }
      } > ...
   < affectation > ...
   < loop > ...
}
} ...
< affectation > ...
< loop > ...
}
}

with

formulation-id:
   string |
   string ~ { expression-cst }

formulation-type:
   FemEquation | etc

local-term-type:
   Integral | deRham

equation-term-sub-type:
   Self (default) | Mutual | SelfAndMutual

quantity-type:
   Local | Global | Integral

term-op-type:
   DtDof | DtDtDof | Eig | JacNL | etc
Note:
1. The optional `Append < expression-cst >` (when the optional level `expression-cst` is strictly positive) permits to append an existing `Formulation` of the same `Name` with additional `Quantity`’s and `Equations`.

2. `IndexOfSystem` permits to resolve ambiguous cases when several quantities belong to the same function space, but to different systems of equations. The integer parameter then specifies the index in the list of an `OriginSystem` command (see Section 5.8 [Resolution], page 38).

3. A `GlobalTerm` defines a term to be assembled in an equation associated with a global quantity. This equation is a finite element equation if that global quantity is linked with local quantities. The optional associated `SubType` defines either self (default) or mutual contributions, or both. Mutual contributions need piecewise functions defined on pairs or regions.

4. A `GlobalEquation` defines a global equation to be assembled in the matrix of the system.

See Section 6.7 [Types for Formulation], page 58, for the complete list of options and Section 7.8 [Formulation examples], page 83, for some examples.

5.8 Resolution: solving systems of equations

The operations available in a `Resolution` include: the generation of a linear system, its solving with various kinds of linear solvers, the saving of the solution or its transfer to another system, the definition of various time stepping methods, the construction of iterative loops for nonlinear problems (Newton-Raphson and fixed point methods), etc. Multi-harmonic resolutions, coupled problems (e.g., magneto-thermal) or linked problems (e.g., pre-computations of source fields) are thus easily defined in GetDP.

The `Resolution` object is characterized by a list of systems to build and their associated formulations, using time or frequency domain, and a list of elementary operations:

```plaintext
Resolution {
  < Append < expression-cst >; >
  Name resolution-id; < Hidden expression-cst; >
  System {
    { Name system-id; NameOfFormulation formulation-list; 
      < Type system-type; >
      < Frequency expression-cst-list-item | 
        Frequency { expression-cst-list }; >
      < DestinationSystem system-id; >
      < OriginSystem system-id; | OriginSystem { system-id <,...> }; >
      < NameOfMesh expression-char > < Solver expression-char >
      < loop > } ... 
    < loop > ... 
  }
  Operation {
    < resolution-op; > ...
    < loop > ...
  }
}
```
with

\begin{verbatim}
resolution-id:
  system-id:
    string | string " { expression-cst }

formulation-list:
  formulation-id <{}> | { formulation-id <{}> <,...> }

system-type:
  Real | Complex

resolution-op:
  Generate[system-id] | Solve[system-id] | etc
\end{verbatim}

Notes:

1. The optional \texttt{Append < expression-cst >} (when the optional level \texttt{expression-cst} is strictly positive) permits to append an existing \texttt{Resolution} of the same \texttt{Name} with additional \texttt{Systems} and \texttt{Operations}.

2. The default type for a system of equations is \texttt{Real}. A frequency domain analysis is defined through the definition of one or several frequencies (\texttt{Frequency expression-cst-list-item | Frequency \{ expression-cst-list \}}). Complex systems of equations with no predefined list of frequencies (e.g., in modal analyses) can be explicitly defined with \texttt{Type Complex}.

3. \texttt{NameOfMesh} permits to explicitly specify the mesh to be used for the construction of the system of equations.

4. \texttt{Solver} permits to explicitly specify the name of the solver parameter file to use for the solving of the system of equations. This is only valid if GetDP was compiled against the default solver library (it is the case if you downloaded a pre-compiled copy of GetDP from the internet).

5. \texttt{DestinationSystem} permits to specify the destination system of a \texttt{TransferSolution} operation (see Section 6.8 [Types for Resolution], page 59).

6. \texttt{OriginSystem} permits to specify the systems from which ambiguous quantity definitions can be solved (see Section 5.7 [Formulation], page 36).

See Section 6.8 [Types for Resolution], page 59, for the complete list of options and Section 7.9 [Resolution examples], page 85, for some examples.

5.9 PostProcessing: exploiting computational results

The \texttt{PostProcessing} object is based on the quantities defined in a \texttt{Formulation} and permits the construction (thanks to the \texttt{expression} syntax) of any useful piecewise defined quantity of interest:
PostProcessing {
  { < Append < expression-cst >; >
    Name post-processing-id;
    NameOfFormulation formulation-id <{}>; < NameOfSystem system-id; >
    Quantity {
      { < Append < expression-cst >; >
        Name post-quantity-id; Value { post-value ... } } ... 
      < loop > ... 
    }
  } ...
  < affectation > ...
  < loop > ...
}

with

  post-processing-id:
  post-quantity-id:
    string | string ~ { expression-cst }

  post-value:
    Local { local-value } | Integral { integral-value }

  local-value:
    [ expression ]; In group-def; Jacobian jacobian-id;

  integral-value:
    [ expression ]; In group-def;
    Integration integration-id; Jacobian jacobian-id;

Notes:

1. The optional Append < expression-cst > (when the optional level expression-cst is strictly positive; its omission fixes it to a top value) permits to append an existing PostProcessing of the same Name with additional Values, or an existing Quantity of the same Name with additional Quantity's. If the Append PostProcessing level is 2, the Append Quantity level is automatically 1 if omitted. Fixing the Append Quantity level to -n suppresses the n lastly defined Quantity's before appending.

2. The quantity defined with integral-value is piecewise defined over the elements of the mesh of group-def, and takes, in each element, the value of the integration of expression over this element. The global integral of expression over a whole region (being either group-def or a subset of group-def) has to be defined in the PostOperation with the post-quantity-id[group-def] command (see Section 5.10 [PostOperation], page 41).

3. If NameOfSystem system-id is not given, the system is automatically selected as the one to which the first quantity listed in the Quantity field of formulation-id is associated.
See Section 6.9 [Types for PostProcessing], page 68, for the complete list of options and Section 7.10 [PostProcessing examples], page 88, for some examples.

### 5.10 PostOperation: exporting results

The PostOperation is the bridge between results obtained with GetDP and the external world. It defines several elementary operations on PostProcessing quantities (e.g., plot on a region, section on a user-defined plane, etc.), and outputs the results in several file formats.

```plaintext
PostOperation {
   { < Append < expression-cst >; >
      Name post-operation-id; NameOfPostProcessing post-processing-id;
      < Hidden expression-cst; >
      < Format post-operation-fmt; >
      < TimeValue expression-cst-list; > < TimeImagValue expression-cst-list; >
      < LastTimeStepOnly < expression-cst >; >
      < OverrideTimeStepValue expression-cst; >
      < NoMesh expression-cst; > < AppendToExistingFile expression-cst; >
      < ResampleTime[expression-cst, expression-cst, expression-cst]; >
      < AppendTimeStepToFileName < expression-cst >; >
   Operation {
      < post-operation-op; > ...
   }
   } ...
   < affectation > ...
   < loop > ...
}
| PostOperation < (Append < expression-cst >) > post-operation-id UsingPost post-processing-id {
   < post-operation-op; > ...
}
```

with

- `post-operation-id`:
  - `string` | `string` ~ `{ expression-cst }

- `post-operation-op`:
  - `Print[ post-quantity-id [group-def], print-support [,print-option] ... ]` |
  - `Print[ expression-list, Format "string" [,print-option] ... ]` |
  - `PrintGroup[ group-id, print-support [,print-option] ... ]` |
  - `Echo[ "string" [,print-option] ... ]` |
  - `CreateDir [ "string" ]` |
  - `DeleteFile [ "string" ]` |
  - `SendMergeFileRequest[ expression-char ]` |
  - `< loop > ...
  etc`
print-support:
OnElementsOf group-def | OnRegion group-def | OnGlobal | etc

print-option:
File expression-char | Format post-operation-fmt | etc

post-operation-fmt:
Table | TimeTable | etc

Notes:
1. The optional Append < expression-cst > (when the optional level expression-cst is strictly positive) permits to append an existing PostOperation of the same Name with additional Operations.
2. Both PostOperation syntaxes are equivalent. The first one conforms to the overall interface, but the second one is more concise.
3. The format post-operation-fmt defined outside the Operation field is applied to all the post-processing operations, unless other formats are explicitly given in these operations with the Format option (see Section 6.10 [Types for PostOperation], page 68). The default format is Gmsh.
4. The ResampleTime option allows equidistant resampling of the time steps by a spline interpolation. The parameters are: start time, stop time, time step.
5. The optional argument [group-def] of the post-quantity-id can only be used when this quantity has been defined as an integral-value (see Section 5.9 [PostProcessing], page 39). In this case, the sum of all elementary integrals is performed over the region group-def.

See Section 6.10 [Types for PostOperation], page 68, for the complete list of options and Section 7.11 [PostOperation examples], page 88, for some examples.
6 Types for objects

This chapter presents the complete list of choices associated with metasyntactic variables introduced for the ten GetDP objects.

6.1 Types for Group

Types in

\texttt{group-type [ R1 <, group-sub-type R2 <, group-sub-type-2 R3 > > ]}

\texttt{group-type < group-sub-type < group-sub-type-2 > > }

- \texttt{Region} Regions in \texttt{R1}.
- \texttt{Global} Regions in \texttt{R1} (variant of \texttt{Region} used with global \texttt{BasisFunctions BF\_Global} and \texttt{BF\_dGlobal}).
- \texttt{NodesOf} Nodes of elements of \texttt{R1}
  \texttt{< Not: but not those of R2 >}.
- \texttt{EdgesOf} Edges of elements of \texttt{R1}
  \texttt{< Not: but not those of R2 >}.
- \texttt{FacetsOf} Facets of elements of \texttt{R1}
  \texttt{< Not: but not those of R2 >}.
- \texttt{VolumesOf} Volumes of elements of \texttt{R1}
  \texttt{< Not: but not those of R2 >}.
- \texttt{ElementsOf} Elements of regions in \texttt{R1}
  \texttt{< OnOneSideOf: only elements on one side of R2 (non-automatic, i.e., both sides if both in R1) > | < OnPositiveSideOf: only elements on positive (normal) side of R2 < , Not: but not those touching only its skin R3 (mandatory for free skins for correct separation of side layers) > >}.
- \texttt{GroupsOfNodesOf} Groups of nodes of elements of \texttt{R1} (a group is associated with each region).
- \texttt{GroupsOfEdgesOf} Groups of edges of elements of \texttt{R1} (a group is associated with each region).
  \texttt{< InSupport: in a support R2 being a group of type ElementOf, i.e., containing elements >}.
- \texttt{GroupsOfEdgesOnNodesOf} Groups of edges incident to nodes of elements of \texttt{R1} (a group is associated with each node).
  \texttt{< Not: but not those of R2 >}.
- \texttt{GroupOfRegionsOf} Single group of elements of regions in \texttt{R1} (with basis function \texttt{BF\_Region} just one DOF is created for all elements of \texttt{R1}).
EdgesOfTreeIn
   Edges of a tree of edges of $R_1$
   \textit{StartingOn}: a complete tree is first built on $R_2$.

FacetsOfTreeIn
   Facets of a tree of facets of $R_1$
   \textit{StartingOn}: a complete tree is first built on $R_2$.

DualNodesOf
   Dual nodes of elements of $R_1$.

DualEdgesOf
   Dual edges of elements of $R_1$.

DualFacetsOf
   Dual facets of elements of $R_1$.

DualVolumesOf
   Dual volumes of elements of $R_1$.

6.2 Types for Function

6.2.1 Math functions

The following functions are the equivalent of the functions of the C or C++ math library. Unless indicated otherwise, arguments to these functions can be real or complex valued when used in expressions. When used in constant expressions (\textit{expression-cst}, see Section 4.4 [Constants], page 16), only real-valued arguments are accepted.

\textit{math-function-id}: 

\textbf{Exp} \ [\textit{expression}]
Exponential function: $e^{expression}$.

\textbf{Log} \ [\textit{expression}]
Natural logarithm: $\ln(expression)$, $expression>0$.

\textbf{Log10} \ [\textit{expression}]
Base 10 logarithm: $\log_{10}(expression)$, $expression>0$.

\textbf{Sqrt} \ [\textit{expression}]
Square root, $expression\geq 0$.

\textbf{Sin} \ [\textit{expression}]
Sine of $expression$.

\textbf{Asin} \ [\textit{expression}]
Arc sine (inverse sine) of $expression$ in $[-\pi/2,\pi/2]$, $expression$ in $[-1,1]$ (real valued only).

\textbf{Cos} \ [\textit{expression}]
Cosine of $expression$. 

Acos [expression]
Arc cosine (inverse cosine) of expression in [0,π], expression in [-1,1] (real valued only).

Tan [expression]
Tangent of expression.

Atan [expression]
Arc tangent (inverse tangent) of expression in [-π/2,π/2] (real valued only).

Atan2 [expression, expression]
Arc tangent (inverse tangent) of the first expression divided by the second, in [-π,π] (real valued only).

Sinh [expression]
Hyperbolic sine of expression.

Cosh [expression]
Hyperbolic cosine of expression.

Tanh [expression]
Hyperbolic tangent of the real valued expression.

TanhC2 [expression]
Hyperbolic tangent of a complex valued expression.

Fabs [expression]
Absolute value of expression (real valued only).

Abs [expression]
Absolute value of expression.

Floor [expression]
Rounds downwards to the nearest integer that is not greater than expression (real valued only).

Ceil [expression]
Rounds upwards to the nearest integer that is not less than expression (real valued only).

Fmod [expression, expression]
Remainder of the division of the first expression by the second, with the sign of the first (real valued only).

Min [expression, expression]
Minimum of the two (scalar) expressions (real valued only).

Max [expression, expression]
Maximum of the two (scalar) expressions (real valued only).

Sign [expression]
-1 for expression less than zero and 1 otherwise (real valued only).
Jn [expression]
Returns the Bessel function of the first kind of order given by the first expression for the value of the second expression (real valued only).

dJn [expression]
Returns the derivative of the Bessel function of the first kind of order given by the first expression for the value of the second expression (real valued only).

Yn [expression]
Returns the Bessel function of the second kind of order given by the first expression for the value of the second expression (real valued only).

dYn [expression]
Returns the derivative of the Bessel function of the second kind of order given by the first expression for the value of the second expression (real valued only).

6.2.2 Extended math functions

extended-math-function-id:

Cross [expression,expression]
Cross product of the two arguments; expression must be a vector.

Hypot [expression,expression]
Square root of the sum of the squares of its arguments.

Norm [expression]
Absolute value if expression is a scalar; euclidian norm if expression is a vector.

SquNorm [expression]
Square norm: Norm[expression]^2.

Unit [expression]
Normalization: expression/Norm[expression]. Returns 0 if the norm is smaller than 1.e-30.

Transpose [expression]
Transposition; expression must be a tensor.

Inv [expression]
Inverse of the tensor expression.

Det [expression]
Determinant of the tensor expression.

Rotate [expression,expression,expression,expression]
Rotation of a vector or tensor given by the first expression by the angles in radians given by the last three expression values around the x-, y- and z-axis.

TTrace [expression]
Trace; expression must be a tensor.
Chapter 6: Types for objects

Cos_wt_p []{expression-cst, expression-cst}

The first parameter represents the angular frequency and the second represents the phase. If the type of the current system is Real, \( F_{\text{Cos}_w t_p}[w,p] \) is identical to \( \text{Cos}[w*\$Time+p] \). If the type of the current system is Complex, it is identical to \( \text{Complex}[\text{Cos}[p],\text{Sin}[p]] \).

Sin_wt_p []{expression-cst, expression-cst}

The first parameter represents the angular frequency and the second represents the phase. If the type of the current system is Real, \( F_{\text{Sin}_w t_p}[w,p] \) is identical to \( \text{Sin}[w*\$Time+p] \). If the type of the current system is Complex, it is identical to \( \text{Complex}[\text{Sin}[p],-\text{Cos}[p]] \).

Period [expression]{expression-cst}

\( \text{Fmod}[\text{expression},\text{expression-cst}] + (\text{expression}<0 ? \text{expression-cst} : 0) \); the result is always in \([0,\text{expression-cst}]\).

Interval [expression, expression, expression]{expression-cst, expression-cst, expression-cst}

Not documented yet.

6.2.3 Green functions

The Green functions are only used in integral quantities (see Section 5.7 [Formulation], page 36). The first parameter represents the dimension of the problem:

- **1D**: \( r = \text{Fabs}[$X-$XS] \)
- **2D**: \( r = \sqrt{[(X-$XS)^2+(Y-$YS)^2]} \)
- **3D**: \( r = \sqrt{[(X-$XS)^2+(Y-$YS)^2+(Z-$ZS)^2]} \)

The triplets of values given in the definitions below correspond to the 1D, 2D and 3D cases.

**green-function-id**:

Laplace []{expression-cst}

\( r/2, 1/(2\pi)*\ln(1/r), 1/(4\pi*r) \).

GradLaplace []{expression-cst}

Gradient of \( \text{Laplace} \) relative to the destination point \( (X, Y, Z) \).

Helmholtz []{expression-cst, expression-cst}

\( \exp(j*k0*r)/(4\pi*r) \), where \( k0 \) is given by the second parameter.

GradHelmholtz []{expression-cst, expression-cst}

Gradient of \( \text{Helmholtz} \) relative to the destination point \( (X, Y, Z) \).
6.2.4 Type manipulation functions

type-function-id:

Complex  [expression-list]
  Creates a (multi-harmonic) complex expression from an number of real-valued
  expressions. The number of expressions in expression-list must be even.

Complex_MH  [expression-list]{expression-cst-list}
  Not documented yet.

Re  [expression]
  Takes the real part of a complex-valued expression.

Im  [expression]
  Takes the imaginary part of a complex-valued expression.

Conj  [expression]
  Computes the conjugate of a complex-valued expression.

Cart2Pol  [expression]
  Converts the cartesian form (real, imaginary) of a complex-valued expression
  into polar form (amplitude, phase [radians]).

Vector  [expression,expression,expression]
  Creates a vector from 3 scalars.

Tensor  [expression,expression,expression,expression,expression,expression,expression,
  expression,expression,expression]
  Creates a second-rank tensor of order 3 from 9 scalars, by row:
    [ scalar0 scalar1 scalar2 ] [ CompXX CompXY CompXZ ]
    T = [ scalar3 scalar4 scalar5 ] = [ CompYX CompYY CompYZ ]
    [ scalar6 scalar7 scalar8 ] [ CompZX CompZY CompZZ ]

TensorV  [expression,expression,expression]
  Creates a second-rank tensor of order 3 from 3 row vectors:
    [ vector0 ]
    T = [ vector1 ]
    [ vector2 ]

TensorSym  [expression,expression,expression,expression,expression,expression,expression]
  Creates a symmetrical second-rank tensor of order 3 from 6 scalars.

TensorDiag  [expression,expression,expression]
  Creates a diagonal second-rank tensor of order 3 from 3 scalars.

SquDyadicProduct  [expression]
  Dyadic product of the vector given by expression with itself.
CompX [expression]
 Gets the X component of a vector.

CompY [expression]
 Gets the Y component of a vector.

CompZ [expression]
 Gets the Z component of a vector.

CompXX [expression]
 Gets the XX component of a tensor.

CompXY [expression]
 Gets the XY component of a tensor.

CompXZ [expression]
 Gets the XZ component of a tensor.

CompYX [expression]
 Gets the YX component of a tensor.

CompYY [expression]
 Gets the YY component of a tensor.

CompYZ [expression]
 Gets the YZ component of a tensor.

CompZX [expression]
 Gets the ZX component of a tensor.

CompZY [expression]
 Gets the ZY component of a tensor.

CompZZ [expression]
 Gets the ZZ component of a tensor.

Cart2Sph [expression]
 Gets the tensor for transformation of vector from cartesian to spherical coordinates.

Cart2Cyl [expression]
 Gets the tensor for transformation of vector from cartesian to cylindric coordinates. E.g. to convert a vector with (x,y,z)-components to one with (radial, tangential, axial)-components: Cart2Cyl[XYZ][] * vector

UnitVectorX
 []
 Creates a unit vector in x-direction.

UnitVectorY
 []
 Creates a unit vector in y-direction.
UnitVectorZ
    []
    Creates a unit vector in z-direction.

6.2.5 Coordinate functions

coord-function-id:

X   []
    Gets the X coordinate.

Y   []
    Gets the Y coordinate.

Z   []
    Gets the Z coordinate.

XYZ  []
    Gets X, Y and Z in a vector.

6.2.6 Miscellaneous functions

misc-function-id:

Printf   [expression]
    Prints the value of expression when evaluated. (MPI_Printf can be use instead, to print the message for all MPI ranks.)

Rand    [expression]
    Returns a pseudo-random number in [0, expression].

Normal   []
    Computes the normal to the element.

NormalSource
    []
    Computes the normal to the source element (only valid in a quantity of Integral type).

Tangent  []
    Computes the tangent to the element (only valid for line elements).

TangentSource
    []
    Computes the tangent to the source element (only valid in a quantity of Integral type and only for line elements).

ElementVol
    []
    Computes the element’s volume.
SurfaceArea
   []{expression-cst-list}
   Computes the area of the physical surfaces in expression-cst-list or of the actual
   surface if expression-cst-list is empty.

GetVolume
   []
   Computes the volume of the actual physical group.

CompElementNum
   []
   Returns 0 if the current element and the current source element are identical.

GetNumElements
   []{expression-cst-list}
   Counts the elements of physical numbers in expression-cst-list or of the actual
   region if expression-cst-list is empty.

ElementNum
   []
   Returns the tag (number) of the current element.

QuadraturePointIndex
   []
   Returns the index of the current quadrature point.

AtIndex [expression]{expression-cst-list}
   Returns the i-th entry of expression-cst-list. This can be used to get an element
   in a list, using an index that is computed at runtime.

InterpolationLinear
   [expression]{expression-cst-list}
   Linear interpolation of points. The number of constant expressions in
   expression-cst-list must be even.

dInterpolationLinear
   [expression]{expression-cst-list}
   Derivative of linear interpolation of points. The number of constant expressions
   in expression-cst-list must be even.

InterpolationBilinear
   [expression, expression]{expression-cst-list}
   Bilinear interpolation of a table based on two variables.

dInterpolationBilinear
   [expression, expression]{expression-cst-list}
   Derivative of bilinear interpolation of a table based on two variables. The result
   is a vector.

InterpolationAkima
   [expression]{expression-cst-list}
Akima interpolation of points. The number of constant expressions in
expression-cst-list must be even.

\[ \text{dInterpolationAkima} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Derivative of Akima interpolation of points. The number of constant expres-
sions in expression-cst-list must be even.

\[ \text{Order} \]
\[
[\text{quantity}]
\]
Returns the interpolation order of the quantity.

\[ \text{Field} \]
\[
[\text{expression}]
\]
Evaluate the last one of the fields (“views”) loaded with \text{GmshRead} (see
Section 6.8 [Types for Resolution], page 59), at the point \text{expression}. Common
usage is thus \text{Field}[\text{XYZ[]}].

\[ \text{Field} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but evaluate all the fields corresponding to the tags in the list, and sum
all the values. A field having no value at the given position does not produce
an error: its contribution to the sum is simply zero.

\[ \text{ScalarField} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but consider only real-valued scalar fields. A second optional argument
is the value of the time step. A third optional argument is a boolean flag to
indicate that the interpolation should be performed (if possible) in the same
element as the current element.

\[ \text{VectorField} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but consider only real-valued vector fields. Optional arguments are
treated in the same way as for \text{ScalarField}.

\[ \text{TensorField} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but consider only real-valued tensor fields. Optional arguments are
treated in the same way as for \text{ScalarField}.

\[ \text{ComplexScalarField} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but consider only complex-valued scalar fields. Optional arguments are
treated in the same way as for \text{ScalarField}.

\[ \text{ComplexVectorField} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but consider only complex-valued vector fields. Optional arguments are
treated in the same way as for \text{ScalarField}.

\[ \text{ComplexTensorField} \]
\[
[\text{expression}]\{\text{expression-cst-list}\}
\]
Idem, but consider only complex-valued tensor fields. Optional arguments are
treated in the same way as for \text{ScalarField}.
GetCpuTime

[]

Returns current CPU time, in seconds (total amount of time spent executing in user mode since GetDP was started).

GetWallClockTime

[]

Returns the current wall clock time, in seconds (total wall clock time since GetDP was started).

GetMemory

[]

Returns the current memory usage, in megabytes (maximum resident set size).

SetNumberRunTime

[expression]{char-expression}

Sets the char-expression ONELAB variable at run-time to expression.

SetNumberRunTimeWithChoices

[expression]{char-expression}

Same as SetNumberRunTime, but adds the value to the choices of the ONELAB variable (i.e. in the same way as SendToServer in PostOperation, which are used for plotting the history of the variable).

GetNumberRunTime

[ <expression> ]{char-expression}

Gets the value of the char-expression ONELAB variable at run-time. If the optional expression is provided, it is used as a default value if ONELAB is not available.

SetVariable

[ expression <,...> ]{ $variable-id }

Sets the value of the runtime variable $variable-id to the value of the first expression, and returns this value. If optional expressions are provided, they are appended to the variable name, separated by _.

GetVariable

[ <expression> <,...> ]{ $variable-id }

Gets the value of the runtime variable $variable-id. If the optional expressions are provided, they are appended to the variable name, separated by _.

ValueFromIndex

[ ]{ expression-cst-list }

Treats expression-cst-list as a map of (entity, value) pairs. Useful to specify nodal or element-wise constraints, where entity is the node (mesh vertex) or element number (tag).

VectorFromIndex

[ ]{ expression-cst-list }

Same ValueFromIndex, but with 3 scalar values per entity.
ValueFromTable
  [ expression ]{ char-expression }
Accesses the map char-expression created by a NodeTable or ElementTable
PostOperation. If the map is not available (e.g. in pre-processing), or if the
entity is not found in the map, use expression as default value. Useful to specify
nodal or element-wise constraints, where entity is the node (mesh vertex) or
element number (tag).

6.3 Types for Constraint

constraint-type:

Assign   To assign a value (e.g., for boundary condition).
Init      To give an initial value (e.g., initial value in a time domain analysis). If two
values are provided (with Value [ expression, expression  ]), the first value
can be used using the InitSolution1 operation. This is mainly useful for the
Newmark time-stepping scheme.

AssignFromResolution
   To assign a value to be computed by a pre-resolution.

InitFromResolution
   To give an initial value to be computed by a pre-resolution.

Network   To describe the node connections of branches in a network.

Link      To define links between degrees of freedom in the constrained region with de-
grees of freedom in a “reference” region, with some coefficient. For example,
to link the degrees of freedom in the constrained region Left with the degrees
of freedom in the reference region Right, located Pi units to the right of the
region Left along the X-axis, with the coefficient -1, one could write:

    { Name periodic;
      Case {
        { Region Left; Type Link ; RegionRef Right;
          Coefficient -1; Function Vector[X[]+Pi, Y[], Z[]] ;
          < FunctionRef XYZ[]; >
        }
      }
    }

In this example, Function defines the mapping that translates the geometrical
elements in the region Left by Pi units along the X-axis, so that they correspond
with the elements in the reference region Right. For this mapping to work,
the meshes of Left and Right must be identical. (The optional FunctionRef
function allows to transform the reference region, useful e.g. to avoid generating
overlapping meshes for rotational links.)

LinkCplx   To define complex-valued links between degrees of freedom. The syntax is the
same as for constraints of type Link, but Coefficient can be complex.
6.4 Types for FunctionSpace

*function-space-type:*

- **Form0**: 0-form, i.e., scalar field of potential type.
- **Form1**: 1-form, i.e., curl-conform field (associated with a curl).
- **Form2**: 2-form, i.e., div-conform field (associated with a divergence).
- **Form3**: 3-form, i.e., scalar field of density type.
- **Form1P**: 1-form perpendicular to the $z=0$ plane, i.e., perpendicular curl-conform field (associated with a curl).
- **Form2P**: 2-form in the $z=0$ plane, i.e., parallel div-conform field (associated with a divergence).
- **Scalar**: Scalar field.
- **Vector**: Vector field.

*basis-function-type:*

- **BF_Node**: Nodal function (on NodesOf, value Form0).
- **BF_Edge**: Edge function (on EdgesOf, value Form1).
- **BF_Facet**: Facet function (on FacetsOf, value Form2).
- **BF_Volume**: Volume function (on VolumesOf, value Form3).
- **BF_GradNode**: Gradient of nodal function (on NodesOf, value Form1).
- **BF_CurlEdge**: Curl of edge function (on EdgesOf, value Form2).
- **BF_DivFacet**: Divergence of facet function (on FacetsOf, value Form3).
- **BF_GroupOfNodes**: Sum of nodal functions (on GroupsOfNodesOf, value Form0).
- **BF_GradGroupOfNodes**: Gradient of sum of nodal functions (on GroupsOfNodesOf, value Form1).
- **BF_GroupOfEdges**: Sum of edge functions (on GroupsOfEdgesOf, value Form1).
- **BF_CurlGroupOfEdges**: Curl of sum of edge functions (on GroupsOfEdgesOf, value Form2).
- **BF_PerpendicularEdge**: 1-form $(0, 0, \text{BF\_Node})$ (on NodesOf, value Form1P).
- **BF_CurlPerpendicularEdge**: Curl of 1-form $(0, 0, \text{BF\_Node})$ (on NodesOf, value Form2P).
BF_GroupOfPerpendicularEdge
  Sum of 1-forms (0, 0, BF_Node) (on NodesOf, value Form1P).

BF_CurlGroupOfPerpendicularEdge
  Curl of sum of 1-forms (0, 0, BF_Node) (on NodesOf, value Form2P).

BF_PerpendicularFacet
  2-form (90 degree rotation of BF_Edge) (on EdgesOf, value Form2P).

BF_DivPerpendicularFacet
  Div of 2-form (90 degree rotation of BF_Edge) (on EdgesOf, value Form3).

BF_Region
  Unit value 1 (on Region or GroupOfRegionsOf, value Scalar).

BF_RegionX
  Unit vector (1, 0, 0) (on Region, value Vector).

BF_RegionY
  Unit vector (0, 1, 0) (on Region, value Vector).

BF_RegionZ
  Unit vector (0, 0, 1) (on Region, value Vector).

BF_Global
  Global pre-computed quantity (on Global, value depends on parameters).

BF_dGlobal
  Exterior derivative of global pre-computed quantity (on Global, value depends
  on parameters).

BF_NodeX
  Vector (BF_Node, 0, 0) (on NodesOf, value Vector).

BF_NodeY
  Vector (0, BF_Node, 0) (on NodesOf, value Vector).

BF_NodeZ
  Vector (0, 0, BF_Node) (on NodesOf, value Vector).

BF_Zero
  Zero value 0 (on all regions, value Scalar).

BF_One
  Unit value 1 (on all regions, value Scalar).

global-quantity-type:
AliasOf
  Another name for a name of coefficient of basis function.
AssociatedWith
  A global quantity associated with a name of coefficient of basis function, and
  therefore with this basis function.

6.5 Types for Jacobian

jacobian-type:
Vol
  Volume Jacobian, for n-D regions in n-D geometries, n = 1, 2 or 3.
Sur
  Surface Jacobian, for (n-1)-D regions in n-D geometries, n = 1, 2 or 3.
Lin
  Line Jacobian, for (n-2)-D regions in n-D geometries, n = 2 or 3.
VolAxi  Axisymmetrical volume Jacobian (1st type: \( r \)), for 2-D regions in axisymmetrical geometries.

SurAxi  Axisymmetrical surface Jacobian (1st type: \( r \)), for 1-D regions in axisymmetrical geometries.

VolAxiSqu Axisymmetrical volume Jacobian (2nd type: \( r^2 \)), for 2-D regions in axisymmetrical geometries.

VolSphShell Volume Jacobian with spherical shell transformation, for \( n \)-D regions in \( n \)-D geometries, \( n = 2 \) or 3.


VolCylShell Volume Jacobian with cylindrical shell transformation, for \( n \)-D regions in \( n \)-D geometries, \( n = 2 \) or 3. For \( n=2 \), VolCylShell is identical to VolSphShell. For \( n=3 \), the axis of the cylinder is supposed to be along the \( z \) axis.


VolAxiSphShell Same as VolAxi, but with spherical shell transformation.


VolAxiSquSphShell Same as VolAxiSqu, but with spherical shell transformation.


VolRectShell Volume Jacobian with rectangular shell transformation, for \( n \)-D regions in \( n \)-D geometries, \( n = 2 \) or 3.


VolAxiRectShell Same as VolAxi, but with rectangular shell transformation.


VolAxiSquRectShell Same as VolAxiSqu, but with rectangular shell transformation.

6.6 Types for Integration

integration-type:

Gauss    Numerical Gauss integration.
GaussLegendre Numerical Gauss integration obtained by application of a multiplicative rule on
the one-dimensional Gauss integration.

element-type:

Line      Line (2 nodes, 1 edge, 1 volume) (#1).
Triangle  Triangle (3 nodes, 3 edges, 1 facet, 1 volume) (#2).
Quadrangle Quadrangle (4 nodes, 4 edges, 1 facet, 1 volume) (#3).
Tetrahedron Tetrahedron (4 nodes, 6 edges, 4 facets, 1 volume) (#4).
Hexahedron Hexahedron (8 nodes, 12 edges, 6 facets, 1 volume) (#5).
Prism     Prism (6 nodes, 9 edges, 5 facets, 1 volume) (#6).
Pyramid   Pyramid (5 nodes, 8 edges, 5 facets, 1 volume) (#7).
Point     Point (1 node) (#15).

Note:
1. $n$ in (#$n$) is the type number of the element (see Section A.1 [Input file format],
   page 111).

6.7 Types for Formulation

formulation-type:

FemEquation Finite element method formulation (all methods of moments, integral methods).

local-term-type:

Integral Integral of Galerkin or Petrov-Galerkin type.
deRham      deRham projection (collocation).

quantity-type:

Local      Local quantity defining a field in a function space. In case a subspace is
considered, its identifier has to be given between the brackets following the
NameOfSpace function-space-id.
Global     Global quantity defining a global quantity from a function space. The identifier
of this quantity has to be given between the brackets following the NameOfSpace
function-space-id.
Integral quantity obtained by the integration of a LocalQuantity before its use in an Equation term.

**term-op-type:**

- **Dt** - Time derivative applied to the whole term of the equation. (Not implemented yet.)
- **DtDof** - Time derivative applied only to the Dof{} term of the equation.
- **DtDt** - Time derivative of 2nd order applied to the whole term of the equation. (Not implemented yet.)
- **DtDtDof** - Time derivative of 2nd order applied only to the Dof{} term of the equation.
- **Eig** - The term is multiplied by (a certain function of) the eigenvalue. This is to be used with the GenerateSeparate and EigenSolve Resolution operations. An optional Order expression; or Rational expression; statement can be added in the term to specify the eigenvalue function. Full documentation of this feature is not available yet.
- **JacNL** - Nonlinear part of the Jacobian matrix (tangent stiffness matrix) to be assembled for nonlinear analysis.
- **DtDofJacNL** - Nonlinear part of the Jacobian matrix for the first order time derivative (tangent mass matrix) to be assembled for nonlinear analysis.
- **NeverDt** - No time scheme applied to the term (e.g., Theta is always 1 even if a theta scheme is applied).

### 6.8 Types for Resolution

**resolution-op:**

- **Generate** [system-id] - Generate the system of equations system-id.
- **Solve** [system-id] - Solve the system of equations system-id.
- **SolveAgain** [system-id] - Save as Solve, but reuses the preconditioner when called multiple times.
- **SetGlobalSolverOptions** [char-expression] - Set global PETSc solver options (with the same syntax as PETSc options specified on the command line, e.g. "-ksp_type gmres -pc_type ilu").
- **GenerateJac** [system-id] - Generate the system of equations system-id using a jacobian matrix (of which the unknowns are corrections dx of the current solution x).
SolveJac  \[[\text{system-id}]\]
Solve the system of equations \(\text{system-id}\) using a jacobian matrix (of which the unknowns are corrections \(dx\) of the current solution \(x\)). Then, Increment the solution \((x=x+dx)\) and compute the relative error \(dx/x\).

GenerateSeparate  \[[\text{system-id}]\]
Generate matrices separately for \(\text{DtDtDof}, \text{DtDof}\) and \(\text{NoDt}\) terms in \(\text{system-id}\). The separate matrices can be used with the \text{Update} operation (for efficient time domain analysis of linear PDEs with constant coefficients), or with the \text{EigenSolve} operation (for solving generalized eigenvalue problems).

GenerateOnly  \[[\text{system-id, expression-cst-list}]\]
Not documented yet.

GenerateOnlyJac  \[[\text{system-id, expression-cst-list}]\]
Not documented yet.

GenerateGroup
Not documented yet.

GenerateRightHandSideGroup
Not documented yet.

Update  \[[\text{system-id}]\]
Update the system of equations \(\text{system-id}\) (built from sub-matrices generated separately with \text{GenerateSeparate}) with the \text{TimeFunction}(s) provided in \text{Assign} constraints. This assumes that the problem is linear, that the matrix coefficients are independent of time, and that all sources are imposed using \text{Assign} constraints.

Update  \[[\text{system-id, expression}]\]
Update the system of equations \(\text{system-id}\) (built from sub-matrices generated separately with \text{GenerateSeparate}) with \text{expression}. This assumes that the problem is linear, that the matrix coefficients are independent of time, and that the right-hand-side of the linear system can simply be multiplied by \text{expression} at each step.

UpdateConstraint  \[[\text{system-id, group-id, constraint-type}]\]
Recompute the constraint of type \text{constraint-type} acting on \text{group-id} during processing.

GetResidual  \[[\text{system-id, }\$\text{variable-id}]\]
Compute the residual \(r = b - A x\) and store its L2 norm in the run-time variable \$\text{variable-id}.\)
GetNormSolution | GetNormRightHandSide | GetNormResidual | GetNormIncrement
[system-id, $variable-id]
Compute the norm of the solution (resp. right-hand-side, residual or increment) and store its L2 norm in the run-time variable $variable-id.

SwapSolutionAndResidual
[system-id]
Swap the solution $x$ and residual $r$ vectors.

SwapSolutionAndRightHandSide
[system-id]
Swap the solution $x$ and right-hand-side $b$ vectors.

InitSolution
[system-id]
Creates a new solution vector, adds it to the solution vector list for system-id, and initializes the solution. The values in the vector are initialized to the values given in a Constraint of Init type (if two values are given in Init, the second value is used). If no constraint is provided, the values are initialized to zero if the solution vector is the first in the solution list; otherwise the values are initialized using the previous solution in the list.

InitSolution1
[system-id]
Same as InitSolution, but uses the first value given in the Init constraints.

CreateSolution
[system-id]
Creates a new solution vector, adds it to the solution vector list for system-id, and initializes the solution to zero.

CreateSolution
[system-id, expression-cst]
Same as CreateSolution, but initialize the solution by copying the expression-cst solution in the solution list.

Apply
[system-id]
x <- Ax

SetSolutionAsRightHandSide
[system-id]
b <- x

SetRightHandSideAsSolution
[system-id]
x <- b

Residual
[system-id]
res <- b - Ax
CopySolution
\([\text{system-id}, \text{char-expression} \mid \text{constant-id}()]\]
Copy the current solution \(x\) into a vector named \text{char-expression} or into a list named \text{constant-id}.

CopySolution
\([\text{char-expression} \mid \text{constant-id}(), \text{system-id}]\]
Copy the vector named \text{char-expression} or the list named \text{constant-id} into the current solution \(x\).

CopyRightHandSide
\([\text{system-id}, \text{char-expression} \mid \text{constant-id}()]\]
Copy the current right-hand side \(b\) into a vector named \text{char-expression} or into a list named \text{constant-id}.

CopyRightHandSide
\([\text{char-expression} \mid \text{constant-id}(), \text{system-id}]\]
Copy the vector named \text{char-expression} or the list named \text{constant-id} into the current right-hand-side \(b\).

CopyResidual
\([\text{system-id}, \text{char-expression} \mid \text{constant-id}()]\]
Copy the current residual into a vector named \text{char-expression} or into a list named \text{constant-id}.

CopyResidual
\([\text{char-expression} \mid \text{constant-id}(), \text{system-id}]\]
Copy the vector named \text{char-expression} or the list named \text{constant-id} into the current residual.

SaveSolution
\([\text{system-id}]\]
Save the solution of the system of equations \text{system-id}.

SaveSolutions
\([\text{system-id}]\]
Save all the solutions available for the system of equations \text{system-id}. This should be used with algorithms that generate more than one solution at once, e.g., \text{EigenSolve} or \text{FourierTransform}.

RemoveLastSolution
\([\text{system-id}]\]
Removes the last solution (i.e. associated with the last time step) associated with system \text{system-id}.

TransferSolution
\([\text{system-id}]\]
Transfer the solution of system \text{system-id}, as an Assign constraint, to the system of equations defined with a DestinationSystem command. This is used with the AssignFromResolution constraint type (see Section 6.3 [Types for Constraint], page 54).
TransferInitSolution
  [system-id]
  Transfer the solution of system system-id, as an Init constraint, to the system of equations defined with a DestinationSystem command. This is used with the InitFromResolution constraint type (see Section 6.3 [Types for Constraint], page 54).

Evaluate [expression <, expression>]
  Evaluate the expression(s).

SetTime [expression]
  Change the current time.

SetTimeStep [expression]
  Change the current time step number (1, 2, 3, ...)

SetDTime [expression]
  Change the current time step value (dt).

SetFrequency [system-id, expression]
  Change the frequency of system system-id.

SystemCommand [expression-char]
  Execute the system command given by expression-char.

Error [expression-char]
  Output error message expression-char.

Test [expression] { resolution-op }
  If expression is true (nonzero), perform the operations in resolution-op.

Test [expression] { resolution-op } { resolution-op }
  If expression is true (nonzero), perform the operations in the first resolution-op, else perform the operations in the second resolution-op.

While [expression] { resolution-op }
  While expression is true (nonzero), perform the operations in resolution-op.

Break []
  Aborts an iterative loop, a time loop or a While loop.

Exit []
  Exit, brutally.

Sleep [expression]
  Sleeps for expression seconds;
SetExtrapolationOrder

[expression-cst]

Chooses the extrapolation order to compute the initialization of the solution vector in time loops. Default is 0.

Print

[ { expression-list } <, File expression-char > <, Format expression-char > ]

Print the expressions listed in expression-list. If Format is given, use it to format the (scalar) expressions like Printf.

Print

[ system-id <, File expression-char > <, { expression-cst-list } > <, TimeStep { expression-cst-list } >]

Print the system system-id. If the expression-cst-list is given, print only the values of the degrees of freedom given in that list. If the TimeStep option is present, limit the printing to the selected time steps.

EigenSolve

[system-id, expression-cst, expression-cst, expression-cst <, expression > ]

Eigenvalue/eigenvector computation using Arpack or SLEPc. The parameters are: the system (which has to be generated with GenerateSeparate[]), the number of eigenvalues/eigenvectors to compute and the real and imaginary spectral shift (around which to look for eigenvalues). The last optional argument allows to filter which eigenvalue/eigenvector pairs will be saved. For example, ($EigenvalueReal > 0) would only keep pairs corresponding to eigenvalues with a strictly positive real part.

Lanczos

[system-id, expression-cst, { expression-cst-list } , expression-cst]

Eigenvalue/eigenvector computation using the Lanczos algorithm. The parameters are: the system (which has to be generated with GenerateSeparate[]), the size of the Lanczos space, the indices of the eigenvalues/eigenvectors to store, the spectral shift. This routine is deprecated: use EigenSolve instead.

FourierTransform

[system-id, system-id, { expression-cst-list }]

On-the-fly (incremental) computation of a Fourier transform. The parameters are: the (time domain) system, the destination system in which the result of the Fourier transfrom is to be saved (it should be declared with Type Complex) and the list of frequencies to consider. The computation is an approximation that assumes that the time step is constant; it is not an actual Discrete Fourier Transform (the number of samples is unknown a priori).

TimeLoopTheta

[expression-cst,expression-cst,expression,expression-cst]    { resolution-op }

Time loop of a theta scheme. The parameters are: the initial time, the end time, the time step and the theta parameter (e.g., 1 for implicit Euler, 0.5 for Crank-Nicolson).
Warning: GetDP automatically handles time-dependent constraints when they are provided using the TimeFunction mechanism in an Assign-type Constraint (see Section 5.3 [Constraint], page 31). However, GetDP cannot automatically transform general time-dependent source terms in weak formulations (time-dependent functions written in a Integral term). Such source terms will be correctly treated only for implicit Euler, as the expression in the Integral term is evaluated at the current time step. For other schemes, the source term should be written explicitly, by splitting it in two ($\theta f_{n+1} + (1-\theta) f_n$), making use of the AtAnteriorTimeStep[] for the second part, and specifying NeverDt in the Integral term.

**TimeLoopNewmark**

[expression-cst,expression-cst,expression,expression-cst,expression-cst]  
{ resolution-op }

Time loop of a Newmark scheme. The parameters are: the initial time, the end time, the time step, the beta and the gamma parameter.

Warning: same restrictions apply for time-dependent functions in the weak formulations as for TimeLoopTheta.

**TimeLoopAdaptive**

[expression-cst,expression-cst,expression-cst,expression-cst,expression-cst,expression-cst,expression-cst,expression-cst-list, System { {system-id,expression-cst,expression-cst,norm-type} ... } | PostOperation { {post-operation-id,expression-cst,expression-cst,norm-type} ... } ]  
{ resolution-op }  
{ resolution-op }

Time loop with variable time steps. The step size is adjusted according the local truncation error (LTE) of the specified Systems/PostOperations via a predictor-corrector method.

The parameters are: start time, end time, initial time step, min. time step, max. time step, integration method, list of breakpoints (time points to be hit). The LTE calculation can be based on all DOFs of a system and/or on a PostOperation result. The parameters here are: System/PostOperation for LTE assessment, relative LTE tolerance, absolute LTE tolerance, norm-type for LTE calculation.

Possible choices for integration-method are: Euler, Trapezoidal, Gear_2, Gear_3, Gear_4, Gear_5, Gear_6. The Gear methods correspond to backward differentiation formulas of order 2..6.

Possible choices for norm-type: L1Norm, MeanL1Norm, L2Norm, MeanL2Norm, LinfNorm.

MeanL1Norm and MeanL2Norm correspond to L1Norm and L2Norm divided by the number of degrees of freedom, respectively.

The first resolution-op is executed every time step. The second one is only executed if the actual time step is accepted (LTE is in the specified range).
E.g. SaveSolution[] is usually placed in the 2nd resolution-op.

IterativeLoop

[expression-cst,expression,expression-cst<,expression-cst>]  { resolution-op }

Iterative loop for nonlinear analysis. The parameters are: the maximum number of iterations (if no convergence), the relaxation factor (multiplies the iterative correction $dx$) and the relative error to achieve. The optional parameter is a flag for testing purposes.

IterativeLoopN

[expression-cst,expression,
System { {system-id,expression-cst,expression-cst, assessed-object norm-type} ... } |
PostOperation { {post-operation-id,expression-cst,expression-cst, norm-type} ... } ]

{ resolution-op }

Similar to IterativeLoop[] but allows to specify in detail the tolerances and the type of norm to be calculated for convergence assessment.

The parameters are: the maximum number of iterations (if no convergence), the relaxation factor (multiplies the iterative correction $dx$). The convergence assessment can be based on all DOFs of a system and/or on a PostOperation result. The parameters here are: System/PostOperation for convergence assessment, relative tolerance, absolute tolerance, assessed object (only applicable for a specified system), norm-type for error calculation.

Possible choices for assessed-object: Solution, Residual, RecalcResidual. Residual assesses the residual from the last iteration whereas RecalcResidual calculates the residual once again after each iteration. This means that with Residual usually one extra iteration is performed, but RecalcResidual causes higher computational effort per iteration. Assessing the residual can only be used for Newton’s method.

Possible choices for norm-type: L1Norm, MeanL1Norm, L2Norm, MeanL2Norm, LinfNorm.

MeanL1Norm and MeanL2Norm correspond to L1Norm and L2Norm divided by the number of degrees of freedom, respectively.

IterativeLinearSolver

Generic iterative linear solver. To be documented.

PostOperation

[post-operation-id]

Perform the specified PostOperation.

GmshRead  [expression-char]

When GetDP is linked with the Gmsh library, read a file using Gmsh. This file can be in any format recognized by Gmsh. If the file contains one or
multiple post-processing fields, these fields will be evaluated using the built-in `Field[]`, `ScalarField[]`, `VectorField[]`, etc., functions (see Section 6.2.6 [Miscellaneous functions], page 50).

(Note that `GmshOpen` and `GmshMerge` can be used instead of `GmshRead` to force Gmsh to do classical “open” and “merge” operations, instead of trying to “be intelligent” when reading post-processing datasets, i.e., creating new models on the fly if necessary.)

`GmshRead [expression-char, expression-cst]`
Same thing as the `GmshRead` command above, except that the field is forced to be stored with the given tag. The tag can be used to retrieve the given field with the built-in `Field[]`, `ScalarField[]`, `VectorField[]`, etc., functions (see Section 6.2.6 [Miscellaneous functions], page 50).

`GmshRead [expression-char, $string]`
Same as the `GmshRead`, but evaluates `expression-char` by replacing a double precision format specifier with the value of the runtime variable `$string`.

`GmshWrite [expression-char, expression-cst]`
Writes the a Gmsh field to disk. (The format is guessed from the file extension.)

`GmshClearAll []`
Clears all Gmsh data (loaded with `GmshRead` and friends).

`DeleteFile [expression-char]`
Delete a file.

`RenameFile [expression-char, expression-char]`
Rename a file.

`CreateDir | CreateDirectory [expression-char]`
Create a directory.

`MPI_SetCommSelf []`
Changes MPI communicator to self.

`MPI_SetCommWorld []`
Changes MPI communicator to world.

`MPI_Barrier []`
MPI barrier (blocks until all processes have reached this call).
MPI_BroadcastFields
[ < expression-list > ]
Broadcast all fields over MPI (except those listed in the list).

MPI_BroadcastVariables
[ ]
Broadcast all runtime variables over MPI.

6.9 Types for PostProcessing

post-value:

Local { local-value }
To compute a local quantity.

Integral { integral-value }
To integrate the expression over each element.

6.10 Types for PostOperation

print-support:

OnElementsOf group-def
To compute a quantity on the elements belonging to the region group-def, where
the solution was computed during the processing stage.

OnRegion group-def
To compute a global quantity associated with the region group-def.

OnGlobal
To compute a global integral quantity, with no associated region.

OnSection
{ { expression-cst-list } { expression-cst-list } { expression-cst-list } }
To compute a quantity on a section of the mesh defined by three points (i.e., on
the intersection of the mesh with a cutting a plane, specified by three points).
Each expression-cst-list must contain exactly three elements (the coordinates
of the points).

OnGrid group-def
To compute a quantity in elements of a mesh which differs from the real support
of the solution. OnGrid group-def differs from OnElementsOf group-def by
the reinterpolation that must be performed.

OnGrid { expression, expression, expression }
{ expression-cst-list-item | { expression-cst-list },
expression-cst-list-item | { expression-cst-list },
expression-cst-list-item | { expression-cst-list } }
To compute a quantity on a parametric grid. The three expressions repres-
ent the three cartesian coordinates x, y and z, and can be functions of the
current values $A$, $B$ and $C$. The values for $A$, $B$ and $C$ are specified
by each expression-cst-list-item or expression-cst-list. For example, \texttt{OnGrid} \{\texttt{Cos[$A$], Sin[$A$], 0}} \{ \texttt{0:2*Pi:Pi/180, 0, 0}} \} will compute the quantity on 360 points equally distributed on a circle in the z=0 plane, and centered on the origin.

\textbf{OnPoint} \{ \texttt{expression-cst-list} \}

To compute a quantity at a point. The expression-cst-list must contain exactly three elements (the coordinates of the point).

\textbf{OnLine} \{ \{ \texttt{expression-cst-list} \} \{ \texttt{expression-cst-list} \} \} \{ \texttt{expression-cst} \}

To compute a quantity along a line (given by its two end points), with an associated number of divisions equal to expression-cst. The interpolation points on the line are equidistant. Each expression-cst-list must contain exactly three elements (the coordinates of the points).

\textbf{OnPlane} \{ \{ \texttt{expression-cst-list} \} \{ \texttt{expression-cst-list} \} \{ \texttt{expression-cst-list} \} \}
\{ \texttt{expression-cst, expression-cst} \}

To compute a quantity on a plane (specified by three points), with an associated number of divisions equal to each expression-cst along both generating directions. Each expression-cst-list must contain exactly three elements (the coordinates of the points).

\textbf{OnBox} \{ \{ \texttt{expression-cst-list} \} \{ \texttt{expression-cst-list} \} \{ \texttt{expression-cst-list} \}
\{ \texttt{expression-cst-list} \} \} \{ \texttt{expression-cst, expression-cst, expression-cst} \}

To compute a quantity in a box (specified by four points), with an associated number of divisions equal to each expression-cst along the three generating directions. Each expression-cst-list must contain exactly three elements (the coordinates of the points).

\textit{print-option}:

\textbf{File} \texttt{expression-char}

Outputs the result in a file named \texttt{expression-char}.

\textbf{File} \texttt{> expression-char}

Same as File \texttt{expression-char}, except that, if several File \texttt{> expression-char} options appear in the same PostOperation, the results are concatenated in the file \texttt{expression-char}.

\textbf{File} \texttt{>> expression-char}

Appends the result to a file named \texttt{expression-char}.

\textbf{AppendToExistingFile} \texttt{expression-cst}

Appends the result to the file specified with File. (Same behavior as \texttt{>} if \texttt{expression-cst} = 1; same behavior as \texttt{>>} if \texttt{expression-cst} = 2.)

\textbf{Name} | \textbf{Label} \texttt{expression-char}

For formats that support it, sets the label of the output field to \texttt{expression-char} (also used with with \texttt{SendToServer} to force the label).
Depth \( \text{expression-cst} \)
Recursive division of the elements if \( \text{expression-cst} \) is greater than zero, derefinement if \( \text{expression-cst} \) is smaller than zero. If \( \text{expression-cst} \) is equal to zero, evaluation at the barycenter of the elements.

AtGaussPoints \( \text{expression-cst} \)
Print result at the specified number of Gauss points.

Skin
Computes the result on the boundary of the region.

Smoothing
\( < \text{expression-cst} > \)
Smoothes the solution at the nodes.

HarmonicToTime \( \text{expression-cst} \)
Converts a harmonic solution into a time-dependent one (with \( \text{expression-cst} \) steps).

Dimension \( \text{expression-cst} \)
Forces the dimension of the elements to consider in an element search. Specifies the problem dimension during an adaptation (h- or p-refinement).

TimeStep \( \text{expression-cst-list-item} | \{ \text{expression-cst-list} \} \)
Outputs results for the specified time steps only.

TimeValue \( \text{expression-cst-list-item} | \{ \text{expression-cst-list} \} \)
Outputs results for the specified time value(s) only.

TimeImagValue \( \text{expression-cst-list-item} | \{ \text{expression-cst-list} \} \)
Outputs results for the specified imaginary time value(s) only.

LastTimeStepOnly
Outputs results for the last time step only (useful when calling a PostOperation directly in a Resolution, for example).

AppendExpressionToFileName \( \text{expression} \)
Evaluate the given \text{expression} at run-time and append it to the filename.

AppendExpressionFormat \( \text{expression-char} \)
C-style format string for printing the \text{expression} provided in AppendExpressionToFileName. Default is "%16g".

AppendTimeStepToFileName \( < \text{expression-cst} > \)
Appends the time step to the output file; only makes sense with LastTimeStepOnly. 
AppendStringToFileName

expression-char

Append the given expression-char to the filename.

OverrideTimeStepValue

expression-cst

Overrides the value of the current time step with the given value.

NoMesh < expression-cst >

Prevents the mesh from being written in the output file (useful with new mesh-based solution formats).

SendToServer

expression-char

Send the value to the Onelab server, using expression-char as the parameter name.

SendToServer

expression-char { expression-cst-list }

Send the requested harmonics of the value to the Onelab server, using expression-char as the parameter name.

Color expression-char

Used with SendToServer, sets the color of the parameter in the Onelab server.

Hidden < expression-cst >

Used with SendToServer, selects the visibility of the exchanged value.

Closed expression-char

Used with SendToServer, closes (or opens) the subtree containing the parameter.

Units expression-char

Used with SendToServer, sets the units of the parameter in the Onelab server.

Frequency

expression-cst-list-item | { expression-cst-list }

Outputs results for the specified frequencies only.

Format post-operation-fmt

Outputs results in the specified format.

Adapt P1 | H1 | H2

Performs p- or h-refinement on the post-processing result, considered as an error map.

Target expression-cst

Specifies the target for the optimizer during adaptation (error for P1|H1, number of elements for H2).
Value  \texttt{expression-cst-list-item} | \{ \texttt{expression-cst-list} \}
Specifies acceptable output values for discrete optimization (e.g. the available interpolation orders with \texttt{Adapt P1}).

Sort  Position | Connection
Sorts the output by position \((x, y, z)\) or by connection (for \texttt{LINE} elements only).

Iso  \texttt{expression-cst}
Outputs directly contour prints (with \texttt{expression-cst} values) instead of elementary values.

Iso  \{ \texttt{expression-cst-list} \}
Outputs directly contour prints for the values specified in the \texttt{expression-cst-list} instead of elementary values.

NoNewLine
Suppresses the new lines in the output when printing global quantities (i.e., with \texttt{Print OnRegion} or \texttt{Print OnGlobal}).

ChangeOfCoordinates
\{ \texttt{expression, expression, expression} \}
Changes the coordinates of the results according to the three expressions given in argument. The three \texttt{expressions} represent the three new cartesian coordinates \(x, y\) and \(z\), and can be functions of the current values of the cartesian coordinates \(\$X, \$Y\) and \(\$Z\).

ChangeOfValues
\{ \texttt{expression-list} \}
Changes the values of the results according to the expressions given in argument. The \texttt{expressions} represent the new values (\(x\)-component, \(y\)-component, etc.), and can be functions of the current values of the solution (\(\$Val0\), \(\$Val1\), etc.).

DecomposeInSimplex
Decomposes all output elements in simplices (points, lines, triangles or tetrahedra).

StoreInVariable
\$\texttt{expression-char}$
Stores the result of a point-wise evaluation or an \texttt{OnRegion} post-processing operation in the run-time variable \$\texttt{code[expression-char]}$.

StoreInRegister
\texttt{expression-cst}
Stores the result of point-wise evaluation or an \texttt{OnRegion} post-processing operation in the register \texttt{expression-cst}.

StoreMinInRegister
\texttt{expression-cst}
Stores the minimum or maximum value of an \texttt{OnElementsOf} post-processing operation in the register \texttt{expression-cst}. 
StoreMinXinRegister
StoreMinYinRegister
StoreMinZinRegister
StoreMaxXinRegister
StoreMaxYinRegister
StoreMaxZinRegister

expression-cst
Stores the X, Y or Z coordinate of the location, where the minimum or maximum of an OnElementsOf post-processing operation occurs, in the register expression-cst.

StoreInField
expression-cst
Stores the result of a post-processing operation in the field (Gmsh list-based post-processing view) with tag expression-cst.

StoreInMeshBasedField
expression-cst
Stores the result of a post-processing operation in the mesh-based field (Gmsh mesh-based post-processing view) with tag expression-cst.

TimeLegend
< { expression, expression, expression } >
Includes a time legend in Gmsh plots. If the three optional expressions giving the position of the legend are not specified, the legend is centered on top of the plot.

FrequencyLegend
< { expression, expression, expression } >
Includes a frequency legend in Gmsh plots. If the three optional expressions giving the position of the legend are not specified, the legend is centered on top of the plot.

EigenvalueLegend
< { expression, expression, expression } >
Includes an eigenvalue legend in Gmsh plots. If the three optional expressions giving the position of the legend are not specified, the legend is centered on top of the plot.

post-operation-fmt:

Gmsh
GmshParsed
Gmsh output. See Section A.1 [Input file format], page 111 and the documentation of Gmsh (http://gmsh.info) for a description of the file formats.

Table
Space oriented column output, e.g., suitable for Gnuplot, Excel, Caleida Graph, etc. The columns are: element-type element-index x-coord y-coord z-coord <x-coord y-coord z-coord> ... real real real values. The three real numbers preceding the values contain context-dependent information, depending on the
type of plot: curvilinear abscissa for **OnLine** plots, normal to the plane for **OnPlane** plots, parametric coordinates for parametric **OnGrid** plots, etc.

**SimpleTable**

Like **Table**, but with only the *x-coord y-coord z-coord* and values columns.

**TimeTable**

Time oriented column output, e.g., suitable for Gnuplot, Excel, Caleida Graph, etc. The columns are: *time-step time x-coord y-coord z-coord <x-coord y-coord z-coord>* . . . value.

**NodeTable**

Table of nodal values, in the form *node-number node-value(s)*. When exported to a file, the total number of nodal values is printed first. The data is automatically exported as a run-time accessible list as well as a ONELAB variable, with the name of the **PostOperation** quantity. The values are also directly usable by the **ValueFromTable** function, which allows to use them as values in a nodal **Constraint**.

**ElementTable**

Table of element values, in the form *element-number element-node-value(s)*. When exported to a file, the total number of element values is printed first. The data is automatically exported as a run-time accessible list as well as a ONELAB variable, with the name of the **PostOperation** quantity. The values are also directly usable by the **ValueFromTable** function, which allows to use them as values in an element-wise **Constraint**.

**Gnuplot**

Space oriented column output similar to the **Table** format, except that a new line is created for each node of each element, with a repetition of the first node if the number of nodes in the element is greater than 2. This permits to draw unstructured meshes and nice three-dimensional elevation plots in Gnuplot. The columns are: *element-type element-index x-coord y-coord z-coord real real real real values*. The three *real* numbers preceding the *values* contain context-dependent information, depending on the type of plot: curvilinear abscissa for **OnLine** plots, normal to the plane for **OnPlane** plots, parametric coordinates for parametric **OnGrid** plots, etc.

**Adaptation**

Adaptation map, suitable for the GetDP `-adapt` command line option.
7 Short examples

7.1 Constant expression examples

The simplest constant expression consists of an integer or a real number as in

\[ 21 \]
\[ -3 \]

or

\[ -3.1415 \]
\[ 27e3 \]
\[ -290.53e-12 \]

Using operators and the classic math functions, constant-ids can be defined:

\[ c1 = \text{Sin}[2/3*3.1415] \times 5000^2; \]
\[ c2 = -1/c1; \]

7.2 Group examples

Let us assume that some elements in the input mesh have the region numbers 1000, 2000 and 3000. In the definitions

\[
\text{Group} \{ \\
\text{Air} = \text{Region}[1000]; \text{Core} = \text{Region}[2000]; \text{Inductor} = \text{Region}[3000]; \\
\text{NonConductingDomain} = \text{Region}[[\text{Air}, \text{Core}]]; \\
\text{ConductingDomain} = \text{Region}[[\text{Inductor}]]; \\
\}
\]

\text{Air}, \text{Core}, \text{Inductor} are identifiers of elementary region groups while \text{NonConductingDomain} and \text{ConductingDomain} are global region groups.

Groups of function type contain lists of entities built on the region groups appearing in their arguments. For example,

\[
\text{NodesOf}[\text{NonConductingDomain}] \\
\text{EdgesOf}[\text{DomainC}, \text{Not SkinDomainC}]
\]

represents the group of nodes of geometrical elements belonging to the regions in \text{NonConductingDomain} and

represents the group of edges of geometrical elements belonging to the regions in \text{DomainC} but not to those of \text{SkinDomainC}.

7.3 Function examples

A physical characteristic is a piecewise defined function. The magnetic permeability \text{mu[]} can for example be defined in the considered regions by

\[
\text{Function} \{ \\
\text{mu}[\text{Air}] = 4.e-7*\text{Pi}; \\
\text{mu}[\text{Core}] = 1000.*4.e-7*\text{Pi}; \\
\}
\]

A nonlinear characteristic can be defined through an expression with arguments, e.g.,
Function {
    mu0 = 4.e-7*Pi;
    a1 = 1000.; b1 = 100.; // Constants
    mu[NonlinearCore] = mu0 + 1./(a1+b1*Norm[$1]^6);
}

where function mu[] in region NonLinearCore has one argument $1 which has to be the magnetic flux density. This function is actually called when writing the equations of a formulation, which permits to directly extend it to a nonlinear form by adding only the necessary arguments. For example, in a magnetic vector potential formulation, one may write $mu[{\text{Curl } a}]$ instead of $mu[]$ in Equation terms (see Section 7.8 [Formulation examples], page 83). Multiple arguments can be specified in a similar way: writing $mu[{\text{Curl } a},{\text{T}}]$ in an Equation term will provide the function $mu[]$ with two usable arguments, $1$ (the magnetic flux density) and $2$ (the temperature).

It is also possible to directly interpolate one-dimensional functions from tabulated data. In the following example, the function $f(x)$ as well as its derivative $f'(x)$ are interpolated from the $(x,f(x))$ couples (0,0.65), (1,0.72), (2,0.98) and (3,1.12):

Function {
    couples = {0, 0.65 , 1, 0.72 , 2, 0.98 , 3, 1.12};
    f[] = InterpolationLinear[$1$]{List[couples]};
    dfdx[] = dInterpolationLinear[$1$]{List[couples]};
}

The function $f[]$ may then be called in an Equation term of a Formulation with one argument $x$. Notice how the list of constants List[couples] is supplied as a list of parameters to the built-in function InterpolationLinear (see Section 4.4 [Constants], page 16, as well as Section 4.6 [Functions], page 22). In order to facilitate the construction of such interpolations, the couples can also be specified in two separate lists, merged with the alternate list ListAlt command (see Section 4.4 [Constants], page 16):

Function {
    data_x = {0, 1, 2, 3};
    data_f = {0.65, 0.72, 0.98, 1.12};
    f[] = InterpolationLinear[$1$]{ListAlt[data_x, data_f]};
    dfdx[] = dInterpolationLinear[$1$]{ListAlt[data_x, data_f]};
}

In order to optimize the evaluation time of complex expressions, registers may be used (see Section 4.9 [Run-time variables and registers], page 24). For example, the evaluation of $g[] = f[\#1]*\text{Sin}[f[\#1]^2]$ would require two (costly) linear interpolations. But the result of the evaluation of $f[]$ may be stored in a register (for example the register 0) with

$g[] = f[\#1]*\text{Sin}[\#0^2]$;

thus reducing the number of evaluations of $f[]$ (and of the argument $\#1$) to one.

The same results can be obtained using a run-time variable $v$:

$g[] = (v = f[\#1])*\text{Sin}[\#0^2]$;

A function can also be time dependent, e.g.,

Function {
    Freq = 50.; Phase = 30./180.*Pi; // Constants
TimeFct_Sin[] = Sin [ 2.*Pi*Freq * $Time + Phase ];
TimeFct_Exp[] = Exp [ - $Time / 0.0119 ];
TimeFct_ExtSin[] = Sin_wt_p [] {2.*Pi*Freq, Phase};

Note that TimeFct_ExtSin[] is identical to TimeFct_Sin[] in a time domain analysis, but also permits to define phasors implicitly in the case of harmonic analyses.

7.4 Constraint examples

Constraints are referred to in FunctionSpaces and are usually used for boundary conditions (Assign type). For example, essential conditions on two surface regions, Surf0 and Surf1, will be first defined by

```
Constraint {
  { Name DirichletBoundaryCondition1; Type Assign;
    Case {
      { Region Surf0; Value 0.; }
      { Region Surf1; Value 1.; }
    }
  }
}
```

The way the Values are associated with Regions (with their nodes, their edges, their global regions, ...) is defined in the FunctionSpaces which use the Constraint. In other words, a Constraint defines data but does not define the method to process them. A time dependent essential boundary condition on Surf1 would be introduced as (cf. Section 7.3 [Function examples], page 75 for the definition of TimeFct_Exp[]):

```
{ Region Surf1; Value 1.; TimeFunction 3*TimeFct_Exp[] }
```

It is important to notice that the time dependence cannot be introduced in the Value field, since the Value is only evaluated once during the pre-processing.

Other constraints can be referred to in Formulations. It is the case of those defining electrical circuit connections (Network type), e.g.,

```
Constraint {
  { Name ElectricalCircuit; Type Network;
    Case Circuit1 {
      { Region VoltageSource; Branch {1,2}; }
      { Region PrimaryCoil; Branch {1,2}; }
    }
    Case Circuit2 {
      { Region SecondaryCoil; Branch {1,2}; }
      { Region Charge; Branch {1,2}; }
    }
  }
}
```

which defines two non-connected circuits (Circuit1 and Circuit2), with an independent numbering of nodes: region VoltageSource is connected in parallel with region PrimaryCoil, and region SecondaryCoil is connected in parallel with region Charge.
7.5 FunctionSpace examples

Various discrete function spaces can be defined in the frame of the finite element method.

7.5.1 Nodal finite element spaces

The most elementary function space is the nodal finite element space, defined on a mesh of a domain \( W \) and denoted \( S^0(W) \) (associated finite elements can be of various geometries), and associated with essential boundary conditions (Dirichlet conditions). It contains 0-forms, i.e., scalar fields of potential type:

\[
v = \sum_{n \in N} v_n s_n \quad v \in S^0(W)
\]

where \( N \) is the set of nodes of \( W \), \( s_n \) is the nodal basis function associated with node \( n \) and \( v_n \) is the value of \( v \) at node \( n \). It is defined by

```plaintext
FunctionSpace {
  { Name Hgrad_v; Type Form0;
    BasisFunction {
      { Name sn; NameOfCoef vn; Function BF_Node;
        Support Domain; Entity NodesOf[All]; }
    }
    Constraint {
      { NameOfCoef vn; EntityType NodesOf;
        NameOfConstraint DirichletBoundaryCondition1; }
    }
  }
}
```

Function \( s_n \) is the built-in basis function BF_Node associated with all nodes (NodesOf) in the mesh of \( W \) (Domain). Previously defined Constraint DirichletBoundaryCondition1 (see Section 7.4 [Constraint examples], page 77) is used as boundary condition.

In the example above, Entity NodesOf[All] is preferred to Entity NodesOf[Domain]. In this way, the list of all the nodes of Domain will not have to be generated. All the nodes of each geometrical element in Support Domain will be directly taken into account.

7.5.2 High order nodal finite element space

Higher order finite elements can be directly taken into account by BF_Node. Hierarchical finite elements for 0-forms can be used by simply adding other basis functions (associated with other geometrical entities, e.g., edges and facets) to BasisFunction, e.g.,

```plaintext
... BasisFunction {
  { Name sn; NameOfCoef vn; Function BF_Node;
    Support Domain; Entity NodesOf[All]; }
  { Name s2; NameOfCoef v2; Function BF_Node_2E;
    Support Domain; Entity EdgesOf[All]; }
}
...
```
7.5.3 Nodal finite element space with floating potentials

A scalar potential with floating values $v_f$ on certain boundaries $G_f, f$ in $C_f$, e.g., for electrostatic problems, can be expressed as

$$v = \sum_{n \in N_v} v_n s_n + \sum_{f \in C_f} v_f s_f \quad v \in S^0(W)$$

where $N_v$ is the set of inner nodes of $W$ and each function $s_f$ is associated with the group of nodes of boundary $G_f, f$ in $C_f$ ($\text{SkinDomainC}$); $s_f$ is the sum of the nodal basis functions of all the nodes of $C_f$. Its function space is defined by

```plaintext
FunctionSpace {
    { Name Hgrad_v_floating; Type Form0;
        BasisFunction {
            { Name sn; NameOfCoef vn; Function BF_Node;
                Support Domain; Entity NodesOf[All, Not SkinDomainC]; }
            { Name sf; NameOfCoef vf; Function BF_GroupOfNodes;
                Support Domain; Entity GroupsOfNodesOf[SkinDomainC]; }
        }
    }
    GlobalQuantity {
        { Name GlobalElectricPotential; Type AliasOf; NameOfCoef vf; }
        { Name GlobalElectricCharge; Type AssociatedWith;
            NameOfCoef vf; }
    }
    Constraint { ... }
}
```

Two global quantities have been associated with this space: the electric potential `GlobalElectricPotential`, being an alias of coefficient $v_f$, and the electric charge `GlobalElectricCharge`, being associated with coefficient $v_f$.

7.5.4 Edge finite element space

Another space is the edge finite element space, denoted $S^1(W)$, containing 1-forms, i.e., curl-conform fields:

$$h = \sum_{e \in E} h_e s_e \quad h \in S^1(W)$$

where $E$ is the set of edges of $W$, $s_e$ is the edge basis function for edge $e$ and $h_e$ is the circulation of $h$ along edge $e$. It is defined by

```plaintext
FunctionSpace {
    { Name Hcurl_h; Type Form1;
        BasisFunction {
            { Name se; NameOfCoef he; Function BF_Edge;
                Support Domain; Entity EdgesOf[All]; }
        }
    }
    Constraint { ... }
}
```
7.5.5 Edge finite element space with gauge condition

A 1-form function space containing vector potentials can be associated with a gauge condition, which can be defined as a constraint, e.g., a zero value is fixed for all circulations along edges of a tree (EdgesOfTreeIn) built in the mesh (Domain), having to be complete on certain boundaries (StartingOn Surf):

```plaintext
Constraint {
  { Name GaugeCondition_a_Mag_3D; Type Assign;
    Case {
      { Region Domain; SubRegion Surf; Value 0.; }
    }
  }
}
```

```plaintext
FunctionSpace {
  { Name Hcurl_a_Gauge; Type Form1;
    BasisFunction {
      { Name se; NameOfCoef ae; Function BF_Edge;
        Support Domain; Entity EdgesOf[All]; }
    }
    Constraint {
      { NameOfCoef ae;
        EntityType EdgesOfTreeIn; EntitySubType StartingOn;
        NameOfConstraint GaugeCondition_a_Mag_3D; }
    }
  }
}
```

7.5.6 Coupled edge and nodal finite element spaces

A 1-form function space, containing curl free fields in certain regions $W_C \setminus (\text{DomainC})$ of $W$, which are the complementary part of $W_C \cap \text{DomainC}$ in $W$, can be explicitly characterized by

$$h = \sum_{k \in E_c} h_k s_k + \sum_{n \in N_c} \phi_n v_n \quad h \in S^1(W)$$

where $E_c$ is the set of inner edges of $W$, $N_c$ is the set of nodes inside $W_C$ and on its boundary $dW_C$, $s_k$ is an edge basis function and $v_n$ is a vector nodal function. Such a space, coupling a vector field with a scalar potential, can be defined by

```plaintext
FunctionSpace {
  { Name Hcurl_hphi; Type Form1;
    BasisFunction {
      { Name sk; NameOfCoef hk; Function BF_Edge;
```
Support DomainC; Entity EdgesOf[All, Not SkinDomainC]; }
{ Name vn; NameOfCoef phin; Function BF_GradNode;
  Support DomainCC; Entity NodesOf[All]; }
{ Name vn; NameOfCoef phic; Function BF_GroupOfEdges;
  Support DomainC; Entity GroupsOfEdgesOnNodesOf[SkinDomainC]; }
}
Constraint {
{ NameOfCoef hk;
  EntityType EdgesOf; NameOfConstraint MagneticField; }
{ NameOfCoef phin;
  EntityType NodesOf; NameOfConstraint MagneticScalarPotential; }
{ NameOfCoef phic;
  EntityType NodesOf; NameOfConstraint MagneticScalarPotential; }
}

This example points out the definition of a piecewise defined basis function, e.g., function \( vn \) being defined with \( BF\_GradNode \) in DomainCC and \( BF\_GroupOfEdges \) in DomainC. This leads to an easy coupling between these regions.

### 7.5.7 Coupled edge and nodal finite element spaces for multiply connected domains

In case a multiply connected domain \( W_{cC} \) is considered, basis functions associated with cuts (\( SurfaceCut \)) have to be added to the previous basis functions, which gives the function space below:

```plaintext
Group {
  _TransitionLayer_SkinDomainC_ =
    ElementsOf[SkinDomainC, OnOneSideOf SurfaceCut];
}

FunctionSpace {
  { Name Hcurl_hphi; Type Form1;
    BasisFunction {
      ... same as above ...

    { Name sc; NameOfCoef Ic; Function BF_GradGroupOfNodes;
      Support ElementsOf[DomainCC, OnOneSideOf SurfaceCut];
      Entity GroupsOfNodesOf[SurfaceCut]; }

    { Name sc; NameOfCoef Icc; Function BF_GroupOfEdges;
      Support DomainC;
      Entity GroupsOfEdgesOf
        [SurfaceCut,
         InSupport _TransitionLayer_SkinDomainC_; ]; }
    }
  }
}
```

GlobalQuantity {

Global quantities associated with the cuts, i.e., currents and voltages if \( h \) is the magnetic field, have also been defined.

### 7.6 Jacobian examples

A simple Jacobian method is for volume transformations (of \( n \)-D regions in \( n \)-D geometries; \( n = 1, 2 \) or \( 3 \)), e.g., in region Domain,

\[
\text{Jacobian} \{ \\
\text{ Name Vol; } \\
\text{ Case } \\
\{ \text{ Region Domain; Jacobian Vol; } \} \\
\}
\]

\textit{Jacobian VolAxi} would define a volume Jacobian for axisymmetrical problems.

A Jacobian method can also be piecewise defined, in \textit{DomainInf}, where an infinite geometrical transformation has to be made using two constant parameters (inner and outer radius of a spherical shell), and in all the other regions (\textit{All}, being the default); in each case, a volume Jacobian is used. This method is defined by:

\[
\text{Jacobian} \{ \\
\text{ Name Vol; } \\
\text{ Case } \\
\{ \text{ Region DomainInf; Jacobian VolSphShell \{Val_Rint, Val_Rext\}; } \\
\{ \text{ Region All; Jacobian Vol; } \} \\
\}
\]
### 7.7 Integration examples

A commonly used numerical integration method is the Gauss integration, with a number of integration points (NumberOfPoints) depending on geometrical element types (GeoElement), i.e.,

```latex
Integration {
  { Name Int_1;
    Case { {Type Gauss;
      Case { { GeoElement Triangle ; NumberOfPoints 4; }
      { GeoElement Quadrangle ; NumberOfPoints 4; }
      { GeoElement Tetrahedron; NumberOfPoints 4; }
      { GeoElement Hexahedron ; NumberOfPoints 6; }
      { GeoElement Prism ; NumberofPoints 9; } }
    }
  }
}
```

The method above is valid for both 2D and 3D problems, for different kinds of elements.

### 7.8 Formulation examples

#### 7.8.1 Electrostatic scalar potential formulation

An electrostatic formulation using an electric scalar potential $v$, i.e.,

\[(\epsilon \nabla v, \nabla v')_W = 0 \quad \forall v' \in S^0(W)\]

is expressed by

```latex
Formulation {
  { Name Electrostatics_v; Type FemEquation;
    Quantity {
      { Name v; Type Local; NameOfSpace Hgrad_v; }
    }
    Equation {
      Integral { [ epsr[] * Dof{Grad v} , {Grad v} ];
        In Domain; Jacobian Vol; Integration Int_1; }
    }
  }
}
```

The density of the Integral term is a copy of the symbolic form of the formulation, i.e., the product of a relative permittivity function $\epsilon$ by a vector of degrees of freedom (Dof{.}); the scalar product of this with the gradient of test function $v$ results in a symmetrical matrix.

Note that another Quantity could be defined for test functions, e.g., $v_p$ defined by `{ Name vp; Type Local; NameOfSpace Hgrad_v; }`. However, its use would result in the computation of a full matrix and consequently in a loss of efficiency.
**7.8.2 Electrostatic scalar potential formulation with floating potentials and electric charges**

An extension of the formulation above can be made to take floating potentials and electrical charges into account (the latter being defined in `FunctionSpace Hgrad_v_floating`), i.e.

```
Formulation {
    { Name Electrostatics_v_floating; Type FemEquation;
        Quantity {
            { Name v; Type Local; NameOfSpace Hgrad_v_floating; }
            { Name V; Type Global;
                NameOfSpace Hgrad_v_floating [GlobalElectricPotential]; }
            { Name Q; Type Global;
                NameOfSpace Hgrad_v_floating [GlobalElectricCharge]; }
        }
        Equation {
            Integral { [ epsr[] * Dof{Grad v} , {Grad v} ]; In Domain; Jacobian Vol; Integration Int_1; }
            GlobalTerm { [ - Dof{Q}/eps0 , {V} ]; In SkinDomainC; }
        }
    }
}
```

with the predefinition Function { eps0 = 8.854187818e-12; }.

**7.8.3 Magnetostatic 3D vector potential formulation**

A magnetostatic 3D vector potential formulation

\[(\nu \text{curl } a, \text{curl } a')_W = (j_s, a')_W, \quad \forall a' \in S^1(W),\]

with a source current density \(j_s\) in inductors \(W_s\), is expressed by

```
Formulation {
    { Name Magnetostatics_a_3D; Type FemEquation;
        Quantity {
            { Name a; Type Local; NameOfSpace Hcurl_a_Gauge; }
        }
        Equation {
            Integral { [ nu[] * Dof{Curl a} , {Curl a} ]; In Domain; Jacobian Vol; Integration Int_1; }
            Integral { [ - SourceCurrentDensity[] , {a} ]; In DomainWithSourceCurrentDensity;
                Jacobian Vol; Integration Int_1; }
        }
    }
}
```

Note that \(j_s\) is here given by a function `SourceCurrentDensity[]`, but could also be given by data computed from another problem, e.g., from an electrokinetic problem (coupling of formulations) or from a fully fixed function space (constraints fixing the density, which is usually more efficient in time domain analyses).
7.8.4 Magnetodynamic 3D or 2D magnetic field and magnetic scalar potential formulation

A magnetodynamic 3D or 2D h-phi formulation, i.e., coupling the magnetic field $h$ with a magnetic scalar potential $phi$, 

$$\partial_t (\mu h, h')_W + (\rho \text{curl} h, \text{curl} h')_{W_c} = 0 \quad \forall h' \in S^1(W)$$

can be expressed by

Formulation {
  { Name Magnetodynamics_hphi; Type FemEquation;
    Quantity {
      { Name h; Type Local; NameOfSpace Hcurl_hphi; }
    }
    Equation {
      Integral { Dt [ \mu[] * Dof{h} , {h} ];
        In Domain; Jacobian Vol; Integration Int_1; }
      Integral { [ \rho[] * Dof{Curl h} , {Curl h} ];
        In DomainC; Jacobian Vol; Integration Int_1; }
    }
  }
}

7.8.5 Nonlinearities, Mixed formulations, ...

In case nonlinear physical characteristics are considered, arguments are used for associated functions, e.g., $\mu[h]$. Several test functions can be considered in an Equation field. Consequently, mixed formulations can be defined.

7.9 Resolution examples

7.9.1 Static resolution (electrostatic problem)

A static resolution, e.g., for the electrostatic formulation (see Section 7.8 [Formulation examples], page 83), can be defined by

Resolution {
  { Name Electrostatics_v;
    System {
      { Name Sys_Ele; NameOfFormulation Electrostatics_v; }
    }
    Operation {
      Generate[Sys_Ele]; Solve[Sys_Ele]; SaveSolution[Sys_Ele];
    }
  }
}

The generation (Generate) of the matrix of the system $Sys_Ele$ will be made with the formulation $Electrostatics_v$, followed by its solving (Solve) and the saving of the solution (SaveSolution).
7.9.2 Frequency domain resolution (magnetodynamic problem)

A frequency domain resolution, e.g., for the magnetodynamic \( h\)-\( \phi \) formulation (see Section 7.8 [Formulation examples], page 83), is given by

\[
\text{Resolution} \{ \\
\quad \text{Name Magnetodynamics}_h\phi; \\
\quad \text{System} \{ \\
\quad \quad \text{Name Sys Mag; NameOfFormulation Magnetodynamics}_h\phi; \\
\quad \quad \quad \text{Frequency Freq}; \} \\
\quad \} \\
\text{Operation} \{ \\
\quad \text{Generate}[\text{Sys Mag}]; \text{Solve}[\text{Sys Mag}]; \text{SaveSolution}[\text{Sys Mag}]; \\
\quad \} \\
\}
\]

preceded by the definition of constant \( \text{Freq} \), e.g.,

\[
\text{Function} \{ \\
\quad \text{Freq} = 50.; \\
\}
\]

7.9.3 Time domain resolution (magnetodynamic problem)

A time domain resolution, e.g., for the same magnetodynamic \( h\)-\( \phi \) formulation (see Section 7.8 [Formulation examples], page 83), is given by

\[
\text{Resolution} \{ \\
\quad \text{Name Magnetodynamics}_h\phi\_Time; \\
\quad \text{System} \{ \\
\quad \quad \text{Name Sys Mag; NameOfFormulation Magnetodynamics}_h\phi; \} \\
\quad \} \\
\text{Operation} \{ \\
\quad \text{InitSolution}[\text{Sys Mag}]; \text{SaveSolution}[\text{Sys Mag}]; \\
\quad \text{TimeLoopTheta}[\text{Mag Time0}, \text{Mag TimeMax}, \text{Mag DTime}, \text{Mag Theta}] \{ \\
\quad \quad \text{Generate}[\text{Sys Mag}]; \text{Solve}[\text{Sys Mag}]; \text{SaveSolution}[\text{Sys Mag}]; \\
\quad \} \\
\quad \} \\
\}
\]

If, e.g., the \text{Resolution} above is preceded by the constant and function definitions below

\[
\text{Function} \{ \\
\quad \text{Tc} = 10.\text{e}-3; \\
\quad \text{Mag Time0} = 0.; \text{Mag TimeMax} = 2.*\text{Tc}; \text{Mag DTime}[] = \text{Tc}/20.; \\
\quad \text{Mag Theta}[] = 1./2.; \\
\}
\]

the performed time domain analysis will be a Crank-Nicolson scheme (theta-scheme with \( \text{Theta} = 0.5 \)) with initial time 0 ms, end time 20 ms and time step 1 ms.
7.9.4 Nonlinear time domain resolution (magnetodynamic problem)

In case a nonlinear problem is solved, an iterative loop has to be defined in an appropriate level of the recursive resolution operations, e.g., for the magnetodynamic problem above,

```
Operation {
    InitSolution[Sys_Mag]; SaveSolution[Sys_Mag];
    TimeLoopTheta[Mag_Time0, Mag_TimeMax, Mag_DTime[], Mag_Theta[]] {
        IterativeLoop[NL_NbrMax, NL_Eps, NL_Relax] {
            GenerateJac[Sys_Mag]; SolveJac[Sys_Mag];
        }
        SaveSolution[Sys_Mag];
    }
}
```

preceded by constant definitions, e.g.,

```
Function {
    NL_Eps = 1.e-4; NL_Relax = 1.; NL_NbrMax = 80;
}
```

7.9.5 Coupled formulations

A coupled problem, e.g., magnetodynamic (in frequency domain; Frequency Freq) - thermal (in time domain) coupling, with temperature dependent characteristics (e.g., rho[T], . . .), can be defined by:

```
Resolution {
    { Name MagnetoThermalCoupling_hphi_T;
        System {
            { Name Sys_Mag; NameOfFormulation Magnetodynamics_hphi;
                Frequency Freq; }
            { Name Sys_The; NameOfFormulation Thermal_T; }
        }
    Operation {
        InitSolution[Sys_Mag]; InitSolution[Sys_The];
        IterativeLoop[NL_NbrMax, NL_Eps, NL_Relax] {
            GenerateJac[Sys_Mag]; SolveJac[Sys_Mag];
            GenerateJac[Sys_The]; SolveJac[Sys_The];
        }
        SaveSolution[Sys_Mag]; SaveSolution[Sys_The];
    }
}
```

Two systems of equations, Sys_Mag and Sys_The, will be solved iteratively until convergence (Criterion), using a relaxation factor (RelaxationFactor).

It can be seen through these examples that many resolutions can be linked or nested directly by the user, which gives a great freedom for coupled problems.
7.10 PostProcessing examples

The quantities to be post-computed based on a solution of a resolution are defined, e.g., for the electrostatic problem (see Section 7.8 [Formulation examples], page 83; see Section 7.9 [Resolution examples], page 85), for the solution associated with the formulation `Electrostatics_v`, by

```plaintext
PostProcessing {
  { Name EleSta_v; NameOfFormulation Electrostatics_v;
    Quantity {
      { Name v; Value { Local { [ {v} ]; In Domain; } } } 
      { Name e; Value { Local { [ -{Grad v} ]; In Domain; } } } 
      { Name d; Value { Local { [ -eps0*epsr[] *{Grad v} ]; In Domain; } } } 
    }
  }
}
```

The electric scalar potential `v` (v), the electric field `e` (e) and the electric flux density `d` (d) can all be computed from the solution. They are all defined in the region `Domain`.

The quantities for the solution associated with the formulation `Electrostatics_v_float` are defined by

```plaintext
PostProcessing {
  { Name EleSta_vf; NameOfFormulation Electrostatics_v_float;
    Quantity {
      ... same as above ...
      
      { Name Q; Value { Local { [ {Q} ]; In SkinDomainC; } } } 
      { Name V; Value { Local { [ {V} ]; In SkinDomainC; } } } 
    }
  }
}
```

which points out the way to define post-quantities based on global quantities.

7.11 PostOperation examples

The simplest post-processing operation is the generation of maps of local quantities, i.e., the display of the computed fields on the mesh. For example, using the `PostProcessing` defined in Section 7.10 [PostProcessing examples], page 88, the maps of the electric scalar potential and of the electric field on the elements of the region `Domain` are defined as:

```plaintext
PostOperation {
  { Name Map_v_e; NameOfPostProcessing EleSta_v ;
    Operation {
      Print [ v, OnElementsOf Domain, File "map_v.pos" ];
      Print [ e, OnElementsOf Domain, File "map_e.pos" ];
    }
  }
}
It is also possible to display local quantities on sections of the mesh, here for example on the plane containing the points (0,0,1), (1,0,1) and (0,1,1):

\[
\text{Print} \ [ \ v, \ \text{OnSection} \ \{ \{0,0,1\} \{1,0,1\} \{0,1,1\} \}, \ \text{File} \ "\text{sec_v.pos}" \ ];
\]

Finally, local quantities can also be interpolated on another mesh than the one on which they have been computed. Six types of grids can be specified for this interpolation: a single point, a set of points evenly distributed on a line, a set of points evenly distributed on a plane, a set of points evenly distributed in a box, a set of points defined by a parametric equation, and a set of elements belonging to a different mesh than the original one:

\[
\text{Print} \ [ \ e, \ \text{OnPoint} \ \{0,0,1\} \ ];
\]
\[
\text{Print} \ [ \ e, \ \text{OnLine} \ \{ \{0,0,1\} \{1,0,1\} \} \{125\} \ ];
\]
\[
\text{Print} \ [ \ e, \ \text{OnPlane} \ \{ \{0,0,1\} \{1,0,1\} \{0,1,1\} \} \{125, \ 75\} \ ];
\]
\[
\text{Print} \ [ \ e, \ \text{OnBox} \ \{ \{0,0,1\} \{1,0,1\} \{0,1,1\} \{0,0,2\} \} \{125, \ 75, \ 85\} \ ];
\]
\[
\text{Print} \ [ \ e, \ \text{OnGrid} \ \{A, \ B, \ 1\} \ {0:1:1/125, \ 0:1:1/75, \ 0}\ ];
\]
\[
\text{Print} \ [ \ e, \ \text{OnGrid} \ \text{Domain2} \ ];
\]

Many options can be used to modify the aspect of all these maps, as well as the default behaviour of the \texttt{Print} commands. See \textit{Section 6.10 [Types for PostOperation]}, page 68, to get the list of all these options. For example, to obtain a map of the scalar potential at the barycenters of the elements on the boundary of the region \texttt{Domain}, in a table oriented format appended to an already existing file \texttt{out.txt}, the operation would be:

\[
\text{Print} \ [ \ v, \ \text{OnElementsOf} \ \texttt{Domain}, \ \text{Depth} \ 0, \ \text{Skin}, \ \text{Format} \ \text{Table}, \ \text{File} \ >> \ "\texttt{out.txt}" \ ];
\]

Global quantities, which are associated with regions (and not with the elements of the mesh of these regions), are displayed thanks to the \texttt{OnRegion} operation. For example, the global potential and charge on the region \texttt{Skin\texttt{DomainC}} can be displayed with:

\[
\text{PostOperation} \ {
\{ \ \text{Name} \ \text{Val}_V \cdot \text{Q}; \ \text{NameOfPostProcessing} \ \text{EleSta}_vf \ ;
\text{Operation} \ {
\text{Print} \ [ \ V, \ \text{OnRegion} \ \texttt{Skin\texttt{DomainC}} \ ];
\text{Print} \ [ \ Q, \ \text{OnRegion} \ \texttt{Skin\texttt{DomainC}} \ ];
\text{\}}
\}
\]
8 Complete examples

This chapter presents complete examples that can be run “as is” with GetDP (see Chapter 3 [Running GetDP], page 11).

Many other ready-to-use examples are available on the website of the ONELAB project: http://onelab.info.

8.1 Electrostatic problem

Let us first consider a simple electrostatic problem. The formulation used is an electric scalar potential formulation (file ‘EleSta_v.pro’, including files ‘Jacobian_Lib.pro’ and ‘Integration_Lib.pro’). It is applied to a microstrip line (file ‘mStrip.pro’), whose geometry is defined in the file ‘mStrip.geo’ (see Appendix B [Gmsh examples], page 115). The geometry is two-dimensional and by symmetry only one half of the structure is modeled.

Note that the structure of the following files points out the separation of the data describing the particular problem and the method used to solve it (see Section 1.1 [Numerical tools as objects], page 5), and therefore how it is possible to build black boxes adapted to well defined categories of problems. The files are commented (see Section 4.1 [Comments], page 15) and can be run without any modification.

/* -------------------------------------------------------------------
File "mStrip.pro"
This file defines the problem dependent data structures for the microstrip problem.

To compute the solution:
getdp mStrip -solve EleSta_v

To compute post-results:
getdp mStrip -pos Map
or getdp mStrip -pos Cut

*-------------------------------------------------------------- */

Group {

/* Let's start by defining the interface (i.e. elementary groups)
   between the mesh file and GetDP (no mesh object is defined, so
   the default mesh will be assumed to be in GMSH format and located
   in "mStrip.msh") */

Air = Region[101]; Diel1 = Region[111];
Ground = Region[120]; Line = Region[121];
SurfInf = Region[130];

/* We can then define a global group (used in "EleSta_v.pro",
the file containing the function spaces and formulations) */

DomainCC_Ele = Region[{Air, Diel1}];
}

Function {

/* The relative permittivity (needed in the formulation) is piecewise
   defined in elementary groups */

epsr[Air] = 1.;
epsr[Diel1] = 9.8;
}

Constraint {

/* Now, some Dirichlet conditions are defined. The name
 'ElectricScalarPotential' refers to the constraint name given in
 the function space */

{ Name ElectricScalarPotential; Type Assign; Case {
Chapter 8: Complete examples

{ Region Region[\{Ground, SurfInf\}]; Value 0.; }
{ Region Line; Value 1.e-3; }

/* The formulation used and its tools, considered as being
in a black box, can now be included */

Include "Jacobian_Lib.pro"
Include "Integration_Lib.pro"
Include "EleSta_v.pro"

/* Finally, we can define some operations to output results */

e = 1.e-7;

PostOperation {
    { Name Map; NameOfPostProcessing EleSta_v;
        Operation {
            Print [ v, OnElementsOf DomainCC_Ele, File "mStrip_v.pos" ];
            Print [ e, OnElementsOf DomainCC_Ele, File "mStrip_e.pos" ];
        }
    }
    { Name Cut; NameOfPostProcessing EleSta_v;
        Operation {
            Print [ e, OnLine \{e,e,0\}{10.e-3,e,0} \{500}, File "Cut_e" ];
        }
    }
}

/* -------------------------------------------------------------------
File "EleSta_v.pro"

Electrostatics - Electric scalar potential \( v \) formulation
-------------------------------------------------------------------

INPUT
-------

Global Groups : (Extension '._Ele' is for Electric problem)

---------
Domain_Ele Whole electric domain (not used)
DomainCC_Ele Nonconducting regions
DomainC_Ele Conducting regions (not used)
Function:
--------
epsr[] Relative permittivity

Constraint:
----------
ElectricScalarPotential Fixed electric scalar potential
(classical boundary condition)

Physical constants:
------------------ */
eps0 = 8.854187818e-12;

Group {
  DefineGroup[ Domain_Ele, DomainCC_Ele, DomainC_Ele ];
}

Function {
  DefineFunction[ epsr ];
}

FunctionSpace {
  { Name Hgrad_v_Ele; Type Form0;
    BasisFunction {
      // v = v s , for all nodes
      // n n
      { Name sn; NameOfCoef vn; Function BF_Node;
        Support DomainCC_Ele; Entity NodesOf[ All ]; } }
    Constraint {
      { NameOfCoef vn; EntityType NodesOf;
        NameOfConstraint ElectricScalarPotential; }
    }
  }
}

Formulation {
  { Name Electrostatics_v; Type FemEquation;
    Quantity {
      { Name v; Type Local; NameOfSpace Hgrad_v_Ele; }
    }
    Equation {
      Galerkin { [ epsr[] * Dof{d v} , {d v} ]; In DomainCC_Ele;
        Jacobian Vol; Integration GradGrad; }
    }
}
Resolution {
  Name EleSta_v;
  System {
    Name Sys_Ele; NameOfFormulation Electrostatics_v; }
  }
  Operation {
    Generate[Sys_Ele]; Solve[Sys_Ele]; SaveSolution[Sys_Ele];
  }
}

PostProcessing {
  Name EleSta_v; NameOfFormulation Electrostatics_v;
  Quantity {
    Name v;
    Value {
      Local { [ {v} ]; In DomainCC_Ele; Jacobian Vol; }
    }
  }
  Name e;
  Value {
    Local { [ -{d v} ]; In DomainCC_Ele; Jacobian Vol; }
  }
  Name d;
  Value {
    Local { [ -eps0*epsr[] * {d v} ]; In DomainCC_Ele;
      Jacobian Vol; }
  }
}

/************************************************************************
File "Jacobian_Lib.pro"

Definition of a jacobian method
************************************************************************/

I N P U T
GlobalGroup :

DomainInf  Regions with Spherical Shell Transformation

Parameters :

Val_Rint, Val_Rext  Inner and outer radius of the Spherical Shell of DomainInf

Group {
  DefineGroup[ DomainInf ] ;
  DefineVariable[ Val_Rint, Val_Rext ] ;
}

Jacobian {
  { Name Vol ;
    Case { { Region DomainInf ;
      Jacobian VolSphShell {Val_Rint, Val_Rext} ; }
    { Region All ; Jacobian Vol ; }
    }
  }
}

/* -------------------------------------------------------------------
File "Integration_Lib.pro"
Definition of integration methods
------------------------------------------------------------------- */

Integration {
  { Name GradGrad ;
    Case { {Type Gauss ;
      Case { { GeoElement Triangle  ; NumberOfPoints 4 ; }
      { GeoElement Quadrangle ; NumberOfPoints 4 ; }
      { GeoElement Tetrahedron  ; NumberOfPoints 4 ; }
      { GeoElement Hexahedron  ; NumberOfPoints 6 ; }
      { GeoElement Prism     ; NumberOfPoints 9 ; }
      }
    }
  }
  { Name CurlCurl ;
    Case { {Type Gauss ;
      Case { { GeoElement Triangle  ; NumberOfPoints 4 ; }
      { GeoElement Quadrangle ; NumberOfPoints 4 ; }
      }
    }
  }
}
{ GeoElement Tetrahedron ; NumberOfPoints 4 ; }
{ GeoElement Hexahedron ; NumberOfPoints 6 ; }
{ GeoElement Prism ; NumberOfPoints 9 ; }
8.2 Magnetostatic problem

We now consider a magnetostatic problem. The formulation used is a 2D magnetic vector potential formulation (see file ‘MagSta_a_2D.pro’). It is applied to a core-inductor system (file ‘CoreSta.pro’), whose geometry is defined in the file ‘Core.geo’ (see Appendix B [Gmsh examples], page 115). The geometry is two-dimensional and, by symmetry, one fourth of the structure is modeled.

The jacobian and integration methods used are the same as for the electrostatic problem presented in Section 8.1 [Electrostatic problem], page 91.

/* --------------------------------------------*/
/* File "CoreSta.pro" */
/* This file defines the problem dependent data structures for the static core-inductor problem. */
/* To compute the solution: */
/* getdp CoreSta -msh Core.msh -solve MagSta_a_2D */
/* To compute post-results: */
/* getdp CoreSta -msh Core.msh -pos Map_a */
/* -------------------------------------------- */

Group {

}
Air = Region[ 101 ]; Core = Region[ 102 ];
Ind = Region[ 103 ]; AirInf = Region[ 111 ];

SurfaceGh0 = Region[ 1100 ]; SurfaceGe0 = Region[ 1101 ];
SurfaceGInf = Region[ 1102 ];

Val_Rint = 200.e-3;
Val_Rext = 250.e-3;

DomainCC_Mag = Region[ {Air, AirInf, Core, Ind} ];
DomainC_Mag = Region[ {} ];
DomainS_Mag = Region[ {Ind} ]; // Stranded inductor
DomainInf = Region[ {AirInf} ];
Domain_Mag = Region[ {DomainCC_Mag, DomainC_Mag} ];

Function {

mu0 = 4.e-7 * Pi;
murCore = 100.;

nu [ Region[{Air, Ind, AirInf}] ] = 1. / mu0;
nu [ Core ] = 1. / (murCore * mu0);

Sc[ Ind ] = 2.5e-2 * 5.e-2;

}

Constraint {

{ Name MagneticVectorPotential_2D;
  Case {
    { Region SurfaceGe0 ; Value 0.; }
    { Region SurfaceGInf; Value 0.; }
  }
}

Val_I_1_ = 0.01 * 1000.;

{ Name SourceCurrentDensityZ;
  Case {
    { Region Ind; Value Val_I_1_/Sc[]; }
  }
}
Include "Jacobian_Lib.pro"
Include "Integration_Lib.pro"
Include "MagSta_a_2D.pro"

\( e = 1.0 \times 10^{-5}; \)
\( p1 = \{ e, e, 0 \}; \)
\( p2 = \{ 0.12, e, 0 \}; \)

\textbf{PostOperation}{

\{ Name Map_a; NameOfPostProcessing MagSta_a_2D;
  Operation{
    Print[ az, OnElementsOf Domain_Mag, File "CoreSta_a.pos" ];
    Print[ b, OnLine\{ List\{ p1 \}\{ List\{ p2 \}\}\\} \{ 1000 \}, File "k_a" ];
  }
\}

}/* ---------------------------------------------------------------------------------------
File "MagSta_a_2D.pro"

Magnetostatics - Magnetic vector potential a formulation (2D)
------------------------------------------------------------------------------

\textbf{INPUT}------------

\textbf{GlobalGroup} : (Extension '_Mag' is for Magnetic problem)
\textbf{-----------}
\textbf{Domain_Mag} \quad \text{Whole magnetic domain}
\textbf{DomainS_Mag} \quad \text{Inductor regions (Source)}

\textbf{Function}  ---
\textbf{-------}
\textbf{nu[]} \quad \text{Magnetic reluctivity}

\textbf{Constraint}  ---
\textbf{-------}
\textbf{MagneticVectorPotential_2D} \quad \text{Fixed magnetic vector potential (2D)}
\quad \quad \text{(classical boundary condition)}
\textbf{SourceCurrentDensityZ} \quad \text{Fixed source current density (in Z direction)}
*/
Group {
  DefineGroup[ Domain_Mag, DomainS_Mag ];
}

Function {
  DefineFunction[ nu ];
}

FunctionSpace {

  // Magnetic vector potential a (b = curl a)
  { Name Hcurl_a_Mag_2D; Type Form1P;
    BasisFunction {
      // a = a s
      // e e
      { Name se; NameOfCoef ae; Function BF_PerpendicularEdge;
        Support Domain_Mag; Entity NodesOf[ All ]; } 
    }
    Constraint {
      { NameOfCoef ae; EntityType NodesOf;
        NameOfConstraint MagneticVectorPotential_2D; } 
    }
  }

  // Source current density js (fully fixed space)
  { Name Hregion_j_Mag_2D; Type Vector;
    BasisFunction {
      { Name sr; NameOfCoef jsr; Function BF_RegionZ;
        Support DomainS_Mag; Entity DomainS_Mag; } 
    }
    Constraint {
      { NameOfCoef jsr; EntityType Region;
        NameOfConstraint SourceCurrentDensityZ; } 
    }
  }
}

Formulation {
  { Name Magnetostatics_a_2D; Type FemEquation;
    Quantity {
      { Name a ; Type Local; NameOfSpace Hcurl_a_Mag_2D; }
      { Name js; Type Local; NameOfSpace Hregion_j_Mag_2D; }
    }
    Equation {
      Galerkin { [ nu[] * Dof{d a} , {d a} ]; In Domain_Mag;
        Jacobian Vol; Integration CurlCurl; } 
    }
}
Galerkin { [ - Dof{js} , {a} ]; In DomainS_Mag; Jacobian Vol; Integration CurlCurl; }
}
}

Resolution {
{ Name MagSta_a_2D;
  System {
    { Name Sys_Mag; NameOfFormulation Magnetostatics_a_2D; }
  }
  Operation {
    Generate[Sys_Mag]; Solve[Sys_Mag]; SaveSolution[Sys_Mag];
  }
}

PostProcessing {
{ Name MagSta_a_2D; NameOfFormulation Magnetostatics_a_2D;
  Quantity {
    { Name a;
      Value {
        Local { [ {a} ]; In Domain_Mag; Jacobian Vol; }
      }
    }
    { Name az;
      Value {
        Local { [ CompZ[{a}] ]; In Domain_Mag; Jacobian Vol; }
      }
    }
    { Name b;
      Value {
        Local { [ {d a} ]; In Domain_Mag; Jacobian Vol; }
      }
    }
    { Name h;
      Value {
        Local { [ nu[] * {d a} ]; In Domain_Mag; Jacobian Vol; }
      }
    }
  }
}
}
8.3 Magnetodynamic problem

As a third example we consider a magnetodynamic problem. The formulation is a two-dimensional a-v formulation (see file 'MagDyn_av_2D.pro', which includes the same jacobian and integration library files as in Section 8.1 [Electrostatic problem], page 91). It is applied to a core-inductor system (defined in file 'CoreMassive.pro'), whose geometry has already been defined in file 'Core.geo'.

/* -------------------------------------------------------------------
 * File "CoreMassive.pro"

This file defines the problem dependent data structures for the dynamic core-inductor problem.

To compute the solution:
    getdp CoreMassive -msh Core.msh -solve MagDyn_av_2D

To compute post-results:
    getdp CoreMassive -msh Core.msh -pos Map_a
    getdp CoreMassive -msh Core.msh -pos U_av
 *--------------------------------------------------------------- */

Group {

    Air   = Region[ 101 ];  Core    = Region[ 102 ];
    Ind   = Region[ 103 ];  AirInf = Region[ 111 ];
    SurfaceGh0 = Region[ 1100 ];  SurfaceGe0 = Region[ 1101 ];
    SurfaceGInf = Region[ 1102 ];

    Val_Rint = 200.e-3;
    Val_Rext = 250.e-3;

    DomainCC_Mag = Region[ {Air, AirInf} ];
    DomainC_Mag  = Region[ {Ind, Core} ];  // Massive inductor + conducting core
    DomainB_Mag  = Region[ {} ];
    DomainS_Mag  = Region[ {} ];
    DomainInf    = Region[ {AirInf} ];
    Domain_Mag   = Region[ {DomainCC_Mag, DomainC_Mag} ];

}

Function {

    mu0 = 4.e-7 * Pi;

    murCore = 100.;
nu [ #{Air, Ind, AirInf} ] = 1. / mu0;
nu [ Core ] = 1. / (murCore * mu0);
sigma [ Ind ] = 5.9e7;
sigma [ Core ] = 2.5e7;

Freq = 1.;

Constraint {

{ Name MagneticVectorPotential_2D;
  Case {
    { Region SurfaceGe0 ; Value 0.; }
    { Region SurfaceGInf; Value 0.; }
  }
}

{ Name SourceCurrentDensityZ;
  Case {
  }
}

Val_I_ = 0.01 * 1000.;

{ Name Current_2D;
  Case {
    { Region Ind; Value Val_I_; }
  }
}

{ Name Voltage_2D;
  Case {
    { Region Core; Value 0.; }
  }
}

Include "Jacobian_Lib.pro"
Include "Integration_Lib.pro"
Include "MagDyn_av_2D.pro"

PostOperation {
  { Name Map_a; NameOfPostProcessing MagDyn_av_2D;
    Operation {


Chapter 8: Complete examples

```plaintext
Print[ az, OnElementsOf Domain_Mag, File "Core_m_a.pos" ];
Print[ j, OnElementsOf Domain_Mag, File "Core_m_j.pos" ];
}
}
{Name U_av; NameOfPostProcessing MagDyn_av_2D;
Operation {
    Print[ U, OnRegion Ind ];
    Print[ I, OnRegion Ind ];
}
}

/* -------------------------------------------------------------------
File "MagDyn_av_2D.pro"
Magnetodynamics - Magnetic vector potential and electric scalar potential a-v formulation (2D)
-------------------------------------------------------------------

INPUT
--------
GlobalGroup : (Extension '_Mag' is for Magnetic problem)
-------------
Domain_Mag Whole magnetic domain
DomainCC_Mag Nonconducting regions (not used)
DomainC_Mag Conducting regions
DomainS_Mag Inductor regions (Source)
DomainV_Mag All regions in movement (for speed term)

Function :
---------
nu[] Magnetic reluctivity
sigma[] Electric conductivity
Velocity[] Velocity of regions

Constraint :
------------
MagneticVectorPotential_2D Fixed magnetic vector potential (2D)
                        (classical boundary condition)
SourceCurrentDensityZ  Fixed source current density (in Z direction)
Voltage_2D Fixed voltage
Current_2D Fixed Current
*/
```
Parameters :
----------

Freq Frequency (Hz)

Parameters for time loop with theta scheme :
Mag_Time0, Mag_TimeMax, Mag_DTime
    Initial time, Maximum time, Time step (s)
Mag_Theta Theta (e.g. 1. : Implicit Euler,
            0.5 : Cranck Nicholson)
*/

Group {
    DefineGroup[ Domain_Mag, DomainCC_Mag, DomainC_Mag,
                  DomainS_Mag, DomainV_Mag ];
}

Function {
    DefineFunction[ nu, sigma ];
    DefineFunction[ Velocity ];
    DefineVariable[ Freq ];
    DefineVariable[ Mag_Time0, Mag_TimeMax, Mag_DTime, Mag_Theta ];
}

FunctionSpace {

    // Magnetic vector potential a (b = curl a)
    { Name Hcurl_a_Mag_2D; Type Form1P;
        BasisFunction {
            // a = a s
            // e e
            { Name se; NameOfCoef ae; Function BF_PerpendicularEdge;
                Support Domain_Mag; Entity NodesOf[ All ]; } }
        Constraint {
            { NameOfCoef ae; EntityType NodesOf;
                NameOfConstraint MagneticVectorPotential_2D; } }
    }

    // Gradient of Electric scalar potential (2D)
    { Name Hregion_u_Mag_2D; Type Form1P;
        BasisFunction {
            { Name sr; NameOfCoef ur; Function BF_RegionZ;
                Support DomainC_Mag; Entity DomainC_Mag; } }
        GlobalQuantity {
            
{ Name U; Type AliasOf; NameOfCoef ur; }
{ Name I; Type AssociatedWith; NameOfCoef ur; }

Constraint {
{ NameOfCoef U; EntityType Region;
  NameOfConstraint Voltage_2D; }
{ NameOfCoef I; EntityType Region;
  NameOfConstraint Current_2D; }
}

// Source current density js (fully fixed space)
{ Name Hregion_j_Mag_2D; Type Vector;
  BasisFunction {
    { Name sr; NameOfCoef jsr; Function BF_RegionZ;
      Support DomainS_Mag; Entity DomainS_Mag; }
  }
  Constraint {
    { NameOfCoef jsr; EntityType Region;
      NameOfConstraint SourceCurrentDensityZ; }
  }
}

Formulation {
{ Name Magnetodynamics_av_2D; Type FemEquation;
  Quantity {
    { Name a; Type Local; NameOfSpace Hcurl_a_Mag_2D; }
    { Name ur; Type Local; NameOfSpace Hregion_u_Mag_2D; }
    { Name I; Type Global; NameOfSpace Hregion_u_Mag_2D [I]; }
    { Name U; Type Global; NameOfSpace Hregion_u_Mag_2D [U]; }
    { Name js; Type Local; NameOfSpace Hregion_j_Mag_2D; }
  }
  Equation {
    Galerkin { [ nu[] * Dof{d a} , {d a} ]; In Domain_Mag;
      Jacobian Vol; Integration CurlCurl; }

    Galerkin { DtDof [ sigma[] * Dof{a} , {a} ]; In DomainC_Mag;
      Jacobian Vol; Integration CurlCurl; }

    Galerkin { [ sigma[] * Dof{ur} , {a} ]; In DomainC_Mag;
      Jacobian Vol; Integration CurlCurl; }

    Galerkin { [ - sigma[] * (Velocity[] *^ Dof{d a}) , {a} ];
      In DomainV_Mag;
      Jacobian Vol; Integration CurlCurl; }
  }
}
Galerkin { [ - Dof{js} , {a} ]; In DomainS_Mag; 
    Jacobian Vol; 
    Integration CurlCurl; }

Galerkin { DtDof [ sigma[] * Dof{a} , {ur} ]; In DomainC_Mag; 
    Jacobian Vol; Integration CurlCurl; }
Galerkin { [ sigma[] * Dof{ur} , {ur} ]; In DomainC_Mag; 
    Jacobian Vol; Integration CurlCurl; }
GlobalTerm { [ Dof{I} , {U} ]; In DomainC_Mag; }

Resolution {
    { Name MagDyn_av_2D;
      System {
        { Name Sys_Mag; NameOfFormulation Magnetodynamics_av_2D;
          Type ComplexValue; Frequency Freq; }
      }
      Operation {
        Generate[Sys_Mag]; Solve[Sys_Mag]; SaveSolution[Sys_Mag];
      }
    }
    { Name MagDyn_t_av_2D;
      System {
        { Name Sys_Mag; NameOfFormulation Magnetodynamics_av_2D; }
      }
      Operation {
        InitSolution[Sys_Mag]; SaveSolution[Sys_Mag];
        TimeLoopTheta[Mag_Time0, Mag_TimeMax, Mag_DTime, Mag_Theta] {
          Generate[Sys_Mag]; Solve[Sys_Mag]; SaveSolution[Sys_Mag];
        }
      }
    }

PostProcessing {
    { Name MagDyn_av_2D; NameOfFormulation Magnetodynamics_av_2D;
      Quantity {
        { Name a;
          Value {
            Local { [ {a} ]; In Domain_Mag; Jacobian Vol; }
          }
        }
      }
    }
}
{ Name az;
    Value {
        Local { [ CompZ[\{a\}] ]; In Domain_Mag; Jacobian Vol; }
    }
}

{ Name b;
    Value {
        Local { [ \{d a\} ]; In Domain_Mag; Jacobian Vol; }
    }
}

{ Name h;
    Value {
        Local { [ nu[] * \{d a\} ]; In Domain_Mag; Jacobian Vol; }
    }
}

{ Name j;
    Value {
        Local { [ - sigma[]*(Dt[\{a\}]+\{ur\}) ]; In DomainC_Mag;
            Jacobian Vol; }
    }
}

{ Name jz;
    Value {
        Local { [ - sigma[]*CompZ[\{a\}]+\{ur\} ]; In DomainC_Mag;
            Jacobian Vol; }
    }
}

{ Name roj2;
    Value {
        Local { [ sigma[]*SquNorm[\{a\}]+\{ur\} ]; In DomainC_Mag;
            Jacobian Vol; }
    }
}

{ Name U; Value { Local { \{U\} }; In DomainC_Mag; }
{ Name I; Value { Local { \{I\} }; In DomainC_Mag; }
}
Appendix A File formats

This chapter describes the file formats that cannot be modified by the user. The format of the problem definition structure is explained in Chapter 5 [Objects], page 29, and Chapter 6 [Types for objects], page 43. The format of the post-processing files is explained in Section 6.10 [Types for PostOperation], page 68.

A.1 Input file format

The native mesh format read by GetDP is the mesh file format produced by Gmsh (http://gmsh.info). In its “version 1” incarnation, an ‘msh’ file is divided into two sections, defining the nodes and the elements in the mesh.

\[
\begin{align*}
\$NOD & \quad \text{number-of-nodes} \\
& \quad \text{node-number } x\text{-coord } y\text{-coord } z\text{-coord} \\
& \quad \ldots \\
\$ENDNOD & \\
\$ELM & \quad \text{number-of-elements} \\
& \quad \text{elm-number } elm\text{-type } elm\text{-region } unused \text{ number-of-nodes } node\text{-numbers} \\
& \quad \ldots \\
\$ENDEL&M
\end{align*}
\]

All the syntactic variables stand for integers except \(x\text{-coord}\), \(y\text{-coord}\) and \(z\text{-coord}\) which stand for floating point values. The \(elm\text{-type}\) value defines the geometrical type for the element:

\[
\begin{align*}
elm\text{-type}: \\
1 & \quad \text{Line (2 nodes, 1 edge).} \\
2 & \quad \text{Triangle (3 nodes, 3 edges).} \\
3 & \quad \text{Quadrangle (4 nodes, 4 edges).} \\
4 & \quad \text{Tetrahedron (4 nodes, 6 edges, 4 facets).} \\
5 & \quad \text{Hexahedron (8 nodes, 12 edges, 6 facets).} \\
6 & \quad \text{Prism (6 nodes, 9 edges, 5 facets).} \\
7 & \quad \text{Pyramid (5 nodes, 8 edges, 5 facets).} \\
15 & \quad \text{Point (1 node).}
\end{align*}
\]

GetDP can also read more recent versions of the ‘msh’ format (2.0 and above), as well as binary meshes. See the Gmsh documentation for more information about these formats.

A.2 Output file format
A.2.1 File ‘.pre’

The ‘.pre’ file is generated by the pre-processing stage. It contains all the information about the degrees of freedom to be considered during the processing stage for a given resolution (i.e., unknowns, fixed values, initial values, etc.).

```
$Resolution /* 'resolution-id' */
main-resolution-number number-of-dofdata
$EndResolution
$DofData /* #dofdata-number */
resolution-number system-number
number-of-function-spaces function-space-number ...
number-of-time-functions time-function-number ...
number-of-partitions partition-index ...
number-of-any-dof number-of-dof
dof-basis-function-number dof-entity dof-harmonic dof-type dof-data
...
$EndDofData
...
```

with

```
dof-data:
equation-number nnz
   (dof-type: 1; unknown) |
dof-value dof-time-function-number
   (dof-type: 2; fixed value) |
dof-associate-dof-number dof-value dof-time-function-number
   (dof-type: 3; associated degree of freedom) |
equation-number dof-value
   (dof-type: 5; initial value for an unknown)
```

Notes:

1. There is one $DofData field for each system of equations considered in the resolution (including those considered in pre-resolutions).
2. The dofdata-number of a $DofData field is determined by the order of this field in the ‘.pre’ file.
3. number-of-dof is the dimension of the considered system of equations, while number-of-any-dof is the total number of degrees of freedom before the application of constraints.
4. Each degree of freedom is coded with three integer values, which are the associated basis function, entity and harmonic numbers, i.e., dof-basis-function-number, dof-entity and dof-harmonic.
5. nnz is not used at the moment.

A.2.2 File ‘.res’

The ‘.res’ file is generated by the processing stage. It contains the solution of the problem (or a part of it in case of program interruption).

```
$ResFormat /* GetDP vgetdp-version-number, string-for-format */
```
1.1 file-res-format
$EndResFormat
$Solution /* DofData #dofdata-number */
  dofdata-number time-value time-imag-value time-step-number
  solution-value
  ...
$EndSolution
  ...

Notes:
1. A $Solution field contains the solution associated with a $DofData field.
2. There is one $Solution field for each time step, of which the time is time-value (0 for non time dependent or non modal analyses) and the imaginary time is time-imag-value (0 for non time dependent or non modal analyses).
3. The order of the solution-values in a $Solution field follows the numbering of the equations given in the `.pre` file (one floating point value for each degree of freedom).
Appendix B Gmsh examples

Gmsh is a three-dimensional finite element mesh generator with simple CAD and post-processing capabilities that can be used as a graphical front-end for GetDP. Gmsh can be downloaded from http://gmsh.info.

This appendix reproduces verbatim the input files needed by Gmsh to produce the mesh files `mStrip.msh` and `Core.msh` used in the examples of Chapter 8 [Complete examples], page 91.

/* -------------------------------------------------------------------
  File "mStrip.geo"

  This file is the geometrical description used by GMSH to produce
  the file "mStrip.msh".

  ------------------------------------------------------------------------- */

/* Definition of some parameters for geometrical dimensions, i.e.
  h (height of 'Diel1'), w (width of 'Line'), t (thickness of 'Line')
  xBox (width of the air box) and yBox (height of the air box) */

h = 1.e-3 ; w = 4.72e-3 ; t = 0.035e-3 ;
xBox = w/2. * 6. ; yBox = h * 12. ;

/* Definition of parameters for local mesh dimensions */

s = 1. ;
p0 = h / 10. * s ;
pLine0 = w/2. / 10. * s ; pLine1 = w/2. / 50. * s ;
pxBox = xBox / 10. * s ; pyBox = yBox / 8. * s ;

/* Definition of geometrical points */

Point(1) = { 0 , 0, 0, p0} ;
Point(2) = { xBox, 0, 0, pxBox} ;
Point(3) = { xBox, h, 0, pxBox} ;
Point(4) = { 0 , h, 0, pLine0} ;
Point(5) = { w/2., h, 0, pLine1} ;
Point(6) = { 0 , h+t, 0, pLine0} ;
Point(7) = { w/2., h+t, 0, pLine1} ;
Point(8) = { 0 , yBox, 0, pyBox} ;
Point(9) = { xBox, yBox, 0, pyBox} ;

/* Definition of geometrical lines */

Line(1) = {1,2} ; Line(2) = {2,3} ; Line(3) = {3,9} ;
Line(4) = {9,8} ; Line(5) = {8,6} ; Line(7) = {4,1} ;
Line(8) = {5,3} ; Line(9) = {4,5} ; Line(10) = {6,7} ;
Line(11) = {5,7};

/* Definition of geometrical surfaces */

Line Loop(12) = {8,-2,-1,-7,9}; Plane Surface(13) = {12};
Line Loop(14) = {10,-11,8,3,4,5}; Plane Surface(15) = {14};

/* Definition of Physical entities (surfaces, lines). The Physical
entities tell GMSH the elements and their associated region numbers
to save in the file 'mStrip.msh'. For example, the Region
111 is made of elements of surface 13, while the Region 121 is
made of elements of lines 9, 10 and 11 */

Physical Surface (101) = {15} ; /* Air */
Physical Surface (111) = {13} ; /* Diel1 */

Physical Line (120) = {1} ; /* Ground */
Physical Line (121) = {9,10,11} ; /* Line */
Physical Line (130) = {2,3,4} ; /* SurfInf */

/* -------------------------------------------------------------------
File "Core.geo"

This file is the geometrical description used by GMSH to produce
the file "Core.msh".
------------------------------------------------------------------- */

dxCore = 50.e-3; dyCore = 100.e-3;
xInd = 75.e-3; dxInd = 25.e-3; dyInd = 50.e-3;
rInt = 200.e-3; rExt = 250.e-3;

s = 1.;
p0 = 12.e-3 *s;
pCorex = 4.e-3 *s; pCorey0 = 8.e-3 *s; pCorey = 4.e-3 *s;
pIndx = 5.e-3 *s; pIndy = 5.e-3 *s;
pInt = 12.5e-3*s; pExt = 12.5e-3*s;

Point(1) = {0,0,0,p0};
Point(2) = {dxCore,0,0,pCorex};
Point(3) = {dxCore,dyCore,0,pCorey};
Point(4) = {0,dyCore,0,pCorey0};
Point(5) = {xInd,0,0,pIndx};
Point(6) = {xInd+dxInd,0,0,pIndx};
Point(7) = {xInd+dxInd,dyInd,0,pIndy};
Point(8) = {xInd,dyInd,0,pIndy};
Point(9) = {rInt,0,0,pInt};
Point(10) = {rExt,0,0,pExt};
Point(11) = {0,rInt,0,pInt};
Point(12) = {0,rExt,0,pExt};

Line(1) = {1,2}; Line(2) = {2,5}; Line(3) = {5,6};
Line(4) = {6,9}; Line(5) = {9,10}; Line(6) = {1,4};
Line(7) = {4,11}; Line(8) = {11,12}; Line(9) = {2,3};
Line(10) = {3,4}; Line(11) = {6,7}; Line(12) = {7,8};
Line(13) = {8,5};

Circle(14) = {9,11,11}; Circle(15) = {10,1,12};

Line Loop(16) = {-6,1,9,10}; Plane Surface(17) = {16};
Line Loop(18) = {11,12,13,3}; Plane Surface(19) = {18};
Line Loop(20) = {7,-14,-4,11,12,13,-2,9,10}; Plane Surface(21) = {20};
Line Loop(22) = {8,-15,-5,14}; Plane Surface(23) = {22};

Physical Surface(101) = {21}; /* Air */
Physical Surface(102) = {17}; /* Core */
Physical Surface(103) = {19}; /* Ind */
Physical Surface(111) = {23}; /* AirInf */

Physical Line(1000) = {1,2}; /* Cut */
Physical Line(1001) = {2}; /* CutAir */
Physical Line(202) = {9,10}; /* SkinCore */
Physical Line(203) = {11,12,13}; /* SkinInd */
Physical Line(1100) = {1,2,3,4,5}; /* SurfaceGh0 */
Physical Line(1101) = {6,7,8}; /* SurfaceGe0 */
Physical Line(1102) = {15}; /* SurfaceGInf */
Appendix C  Compiling the source code

Stable releases and source snapshots are available from http://getdp.info/src/. You can also access the Git repository directly:

1. The first time you want to download the latest full source, type:
   
   ```
   git clone http://gitlab.onelab.info/getdp/getdp.git
   ```

2. To update your local version to the latest and greatest, go in the getdp directory and type:
   
   ```
   git pull
   ```

Once you have the source code, you need to run CMake to configure your build (see the README.txt file in the top-level source directory for detailed information on how to run CMake).

Each build can be configured using a series of options, to selectively enable optional modules or features. Here is the list of CMake options:

- **ENABLE_ARPACK**
  Enable Arpack eigensolver (requires Fortran) (default: ON)

- **ENABLE_CONTRIB_ARPACK**
  Enable Arpack eigensolver from GetDP’s contrib folder (requires Fortran) (default: OFF)

- **ENABLE_BLAS_LAPACK**
  Enable BLAS/Lapack for linear algebra (e.g. for Arpack) (default: ON)

- **ENABLE_BUILD_LIB**
  Enable ’lib’ target for building static GetDP library (default: OFF)

- **ENABLE_BUILD_SHARED**
  Enable ’shared’ target for building shared GetDP library (default: OFF)

- **ENABLE_BUILD_DYNAMIC**
  Enable dynamic GetDP executable (linked with shared lib) (default: OFF)

- **ENABLE_BUILD_ANDROID**
  Enable Android NDK library target (experimental) (default: OFF)

- **ENABLE_BUILD_IOS**
  Enable iOS (ARM) library target (experimental) (default: OFF)

- **ENABLE_FORTRAN**
  Enable Fortran (needed for Arpack/Sparskit/Zitsol & Bessel) (default: ON)

- **ENABLE_GMSH**
  Enable Gmsh functions (for field interpolation) (default: ON)

- **ENABLE_GSL**
  Enable GSL functions (for some built-in functions) (default: ON)

- **ENABLE_HPDDM**
  Enable HPDDM support (default: ON)
ENABLE_KERNEL
    Enable kernel (required for actual computations) (default: ON)

ENABLE_MMA
    Enable MMA optimizer (default: ON)

ENABLE_MPI
    Enable MPI parallelization (with PETSc/SLEPc) (default: OFF)

ENABLE_MULTIHARMONIC
    Enable multi-harmonic support (default: OFF)

ENABLE_NR
    Enable NR functions (if GSL is unavailable) (default: ON)

ENABLE_NX
    Enable proprietary NX extension (default: OFF)

ENABLE_OCTAVE
    Enable Octave functions (default: OFF)

ENABLE_OPENMP
    Enable OpenMP parallelization of some functions (experimental) (default: OFF)

ENABLE_PETSC
    Enable PETSc linear solver (default: ON)

ENABLE_PRIVATE_API
    Enable private API (default: OFF)

ENABLE_PYTHON
    Enable Python functions (default: ON)

ENABLE_SLEPC
    Enable SLEPc eigensolver (default: ON)

ENABLE_SMALLFEM
    Enable experimental SmallFem assembler (default: OFF)

ENABLE_SPARSKIT
    Enable Sparskit solver instead of PETSc (requires Fortran) (default: ON)

ENABLE_PEWE
    Enable PeWe exact solutions (requires Fortran) (default: ON)

ENABLE_WRAP_PYTHON
    Build Python wrappers (default: OFF)

ENABLE_ZITSOL
    Enable Zitsol solvers (requires PETSc and Fortran) (default: OFF)
Appendix D Frequently asked questions

D.1 The basics
1. What is GetDP?
   GetDP is a scientific software environment for the numerical solution of integro-differential equations, open to the coupling of physical problems (electromagnetic, thermal, mechanical, etc) as well as of numerical methods (finite element method, integral methods, etc). It can deal with such problems of various dimensions (1D, 2D, 2D axisymmetric or 3D) and time states (static, transient or harmonic). The main feature of GetDP is the closeness between the organization of data defining discrete problems (written by the user in ASCII data files) and the symbolic mathematical expressions of these problems.

2. What are the terms and conditions of use?
   GetDP is distributed under the terms of the GNU General Public License. See Appendix H [License], page 133 for more information.

3. What does ‘GetDP’ mean?
   It’s an acronym for a “General environment for the treatment of Discrete Problems”.

4. Where can I find more information?
   http://getdp.info is the primary location to obtain information about GetDP. There you will for example find the complete reference manual and the bug tracking database.

D.2 Installation
1. Which OSes does GetDP run on?
   Gmsh runs on Windows, MacOS X, Linux and most Unix variants.

2. What do I need to compile GetDP from the sources?
   You need a C++ and a Fortran compiler as well as the GSL (version 1.2 or higher; freely available from http://sources.redhat.com/gsl).

3. How do I compile GetDP?
   You need cmake (http://www.cmake.org) and a C++ compiler (and a Fortran compiler depending on the modules/solvers you want to compile). See Appendix C [Compiling the source code], page 119 and the README.txt file in the top-level source directory for more information.

   Try ldd getdp (or otool -L getdp on MacOS X) to check if all the required shared libraries are installed on your system. If not, install them. If it still doesn’t work, recompile GetDP from the sources.

D.3 Usage
1. How can I provide a mesh to GetDP?
   The only meshing format accepted by this version of GetDP is the ‘msh’ format created by Gmsh http://gmsh.info. This format being very simple (see the Gmsh reference
manual for more details), it should be straightforward to write a converter from your mesh format to the ‘msh’ format.

2. How can I visualize the results produced by GetDP?

You can specify a format in all post-processing operations. Available formats include Table, SimpleTable, TimeTable and Gmsh. Table, SimpleTable and TimeTable output lists of numbers easily readable by Excel/gnuplot/Caleida Graph/etc. Gmsh outputs post-processing views directly loadable by Gmsh.

3. How do I change the linear solver used by GetDP?

It depends on which linear solver toolkit was enabled when GetDP was compiled (PETSc or Sparskit).

With PETSc-based linear solvers you can either specify options on the command line (e.g. with -ksp_type gmres -pc_type ilu), through a specific option file (with -solver file), through the ‘.petsrc’ file located in your home directly, or directly in the Resolution field using the SetGlobalSolverOptions[] command.

With Sparskit-based linear solvers can either specify options directly on command line (e.g. with -Nb_Fill 200), specify an option file explicitly (with -solver file), or edit the ‘solver.par’ file in the current working directory. If no ‘solver.par’ file exists in the current directory, GetDP will give it the next time you perform a linear system solution.
Appendix E Tips and tricks

- Install the 'info' version of this user’s guide! On your (Unix) system, this can be achieved by 1) copying all getdp.info* files to the place where your info files live (usually /usr/info), and 2) issuing the command 'install-info /usr/info/getdp.info /usr/info/dir'. You will then be able to access the documentation with the command 'info getdp'. Note that particular sections ("nodes") can be accessed directly. For example, 'info getdp functionspace' will take you directly to the definition of the FunctionSpace object.

- Use emacs to edit your files, and load the C++ mode! This permits automatic syntax highlighting and easy indentation. Automatic loading of the C++ mode for `.pro` files can be achieved by adding the following command in your .emacs file: `(setq auto-mode-alist (append '(
"\.
pro\$" . c++-mode)) auto-mode-alist)).

- Define integration and Jacobian method in separate files, reusable in all your problem definition structures (see Section 4.2 [Includes], page 15). Define meshes, groups, functions and constraints in one file dependent of the geometrical model, and function spaces, formulations, resolutions and post-processings in files independent of the geometrical model.

- Use All as soon as possible in the definition of topological entities used as Entity of BasisFunctions. This will prevent GetDP from constructing unnecessary lists of entities.

- Intentionally misspelling an object type in the problem definition structure will produce an error message listing all available types in the particular context.

- If you don’t specify the mandatory arguments on the command line, GetDP will give you the available choices. For example, 'getdp test -pos' (the name of the PostOperation is missing) will produce an error message listing all available PostOperations.
Appendix F Version history

3.3.1 (Work-in-progress): new Min and Max functions on constants (at parse time); fixed regression in trees of edges in 2D; small bug fixes.

3.3.0 (December 21, 2019): improved support for curved elements; added support for auto-similar trees of edges (e.g. for sliding surfaces in 3D); update for latest Gmsh version.

3.2.0 (July 1, 2019): improved node and edge link constraints search using rtree; added support for BF_Edge basis functions on curved elements; small fixes.

3.1.0 (April 19, 2019): added support for high-order (curved) Lagrange elements (P2, P3 and P4); added support for latest Gmsh version; code refactoring.

3.0.4 (December 9, 2018): allow general groups in Jacobian definitions; fixed string parser regression.

3.0.3 (October 18, 2018): new AtGaussPoint PostOperation option; bug fixes.

3.0.2 (September 10, 2018): small compilation fixes.

3.0.1 (September 7, 2018): small bug fixes.

3.0.0 (August 22, 2018): new extrapolation (see SetExtrapolationOrder) in time-domain resolutions; new string macros; added support for Gmsh MSH4 file format; new file handling operations and ElementTable format in PostOperation; added support for curved (2nd order) simplices; enhanced communication of post-processing data with ONELAB; many new functions (Atanh, JnSph, YnSph, ValueFromTable, ListFromServer, GroupExists, ...); various small bug fixes.

2.11.3 (November 5, 2017): new 'Eig' operator for general eigenvalue problems (polynomial, rational); small improvements and bug fixes.

2.11.2 (June 23, 2017): minor build system changes.

2.11.1 (May 13, 2017): small bug fixes and improvements.

2.11.0 (January 3, 2017): small improvements (complex math functions, mutual terms, one side of, get/save runtime variables) and bug fixes.

2.10.0 (October 9, 2016): ONELAB 1.3 with usability and performance improvements.

2.9.2 (August 21, 2016): small bug fixes.
2.9.1 (August 18, 2016): small improvements (CopySolution[], -cpu) and bug fixes.

2.9.0 (July 11, 2016): new ONELAB 1.2 protocol with native support for lists; simple C++ and Python API for exchanging (lists of) numbers and strings; extended .pro language for the construction of extensible problem definitions ("Append"); new VolCylShell transformation; new functions (Min, Max, SetDTime, ...); small fixes.

2.8.0 (March 5, 2016): new Parse[], {Set,Get}{Number,String}[] and OnPositiveSideOf commands; added support for lists of strings; various improvements and bug fixes for better interactive use with ONELAB.

2.7.0 (November 7, 2015): new Else/ElseIf commands; new timing and memory reporting functions.

2.6.1 (July 30, 2015): enhanced Print[] command; minor fixes.

2.6.0 (July 21, 2015): new ability to define and use Macros in .pro files; new run-time variables (act as registers, but with user-defined names starting with '$') and run-time ONELAB Get/Set functions; new Append*ToFileName PostOperation options; new GetResidual and associated operations; fixes and extended format support in MSH file reader; fixed UpdateConstraint for complex-simulated-real and multi-harmonic calculations.

2.5.1 (April 18, 2015): enhanced Python[] and DefineFunction[].

2.5.0 (March 12, 2015): added option to embed Octave and Python interpreters; extended "Field" functions with gradient; extended string and list handling functions; new resolution and postprocessing functions (RenameFile, While, ...); extended EigenSolve with eigenvalue filter and high order polynomial EV problems; small bug fixes.

2.4.4 (July 9, 2014): better stability, updated onelab API version and inline parameter definitions, fixed UpdateConstraint in harmonic case, improved performance of multi-harmonic assembly, fixed memory leak in parallel MPI version, improved EigenSolve (quadratic EVP with SLEPC, EVP on real matrices), new CosineTransform, MPI_Printf, SendMergeFileRequest parser commands, small improvements and bug fixes.

2.4.3 (February 7, 2014): new mandatory 'Name' attribute to define onelab variables in DefineConstant[] & co; minor bug fixes.

2.4.2 (September 27, 2013): fixed function arguments in nested expressions; minor improvements.

2.4.1 (July 16, 2013): minor improvements and bug fixes.
2.4.0 (July 9, 2013): new two-step Init constraints; faster network computation (with new -cache); improved Update operation; better cpu/memory reporting; new -setnumber, -setstring and -gmshread command line options; accept unicode file paths on Windows; small bug fixes.

2.3.1 (May 11, 2013): updated onelab; small bug fixes.

2.3.0 (March 9, 2013): moved build system from autoconf to cmake; new family of Field functions to use data imported from Gmsh; improved list handling; general code cleanup.

2.2.1 (July 15, 2012): cleaned up nonlinear convergence tests and integrated experimental adaptive time loop code; small bug fixes.

2.2.0 (June 19, 2012): new solver interface based on ONELAB; parallel SLEPC eigensolvers; cleaned up syntax for groups, moving band and global basis functions; new Field[] functions to interpolate post-processing datasets from Gmsh; fixed bug in Sur/Lin transformation of 2 forms; fixed bug for periodic constraints on high-order edge elements.

2.1.1 (April 12, 2011): default direct solver using MUMPS.

2.1.0 (October 24, 2010): parallel resolution using PETSc solvers; new Gmsh2 output format; new experimental SLEPC-based eigensolvers; various bug and performance fixes (missing face basis functions, slow PETSc assembly with global quantities, ...)

2.0.0 (March 16, 2010): general code cleanup (separated interface from kernel code; removed various undocumented, unstable and otherwise experimental features; moved to C++); updated input file formats; default solvers are now based on PETSc; small bug fixes (binary .res read, Newmark -restart).

1.2.1 (March 18, 2006): Small fixes.

1.2.0 (March 10, 2006): Windows versions do not depend on Cygwin anymore; major parser cleanup (loops & co).

1.1.2 (September 3, 2005): Small fixes.

1.1.0 (August 21, 2005): New eigensolver based on Arpack (EigenSolve); generalized old Lanczos solver to work with GSL+lapack; reworked PETSc interface, which now requires PETSc 2.3; documented many previously undocumented features (loops, conditionals, strings, link constraints, etc.); various improvements and bug fixes.

1.0.1 (February 6, 2005): Small fixes.
1.0.0 (April 24, 2004): New license (GNU GPL); added support for latest Gmsh mesh file format; more code cleanups.

0.91: Merged moving band and multi-harmonic code; new loops and conditionals in the parser; removed old readline code (just use GNU readline if available); upgraded to latest Gmsh post-processing format; various small enhancements and bug fixes.

0.89 (March 26, 2003): Code cleanup.

0.88: Integrated FMM code.

0.87: Fixed major performance problem on Windows (matrix assembly and post-processing can be up to 3-4 times faster with 0.87 compared to 0.86, bringing performance much closer to Unix versions); fixed stack overflow on Mac OS X; Re-introduced face basis functions mistakenly removed in 0.86; fixed post-processing bug with pyramidal basis functions; new build system based on autoconf.

0.86 (January 25, 2003): Updated Gmsh output format; many small bug fixes.

0.85 (January 21, 2002): Upgraded communication interface with Gmsh; new ChangeOfValues option in PostOperation; many internal changes.

0.84 (September 6, 2001): New ChangeOfCoordinate option in PostOperation; fixed crash in InterpolationAkima; improved interactive postprocessing (-ipos); changed syntax of parametric OnGrid ($S, $T -> $A, $B, $C); corrected Skin for non simplicial meshes; fixed floating point exception in diagonal matrix scaling; many other small fixes and cleanups.

0.83: Fixed bugs in SaveSolutions[] and InitSolution[]; fixed corrupted binary post-processing files in the harmonic case for the Gmsh format; output files are now created relatively to the input file directory; made solver options available on the command line; added optional matrix scaling and changed default parameter file name to 'solver.par' (Warning: please check the scaling definition in your old SOLVER.PAR files); generalized syntax for lists (start:[incr]end -> start:end:incr); updated reference guide; added a new short presentation on the web site; OnCut -> OnSection; new functional syntax for resolution operations (e.g. Generate X -> Generate[X]) many other small fixes and cleanups.

0.82: Added communication socket for interactive use with Gmsh; corrected (again) memory problem (leak + seg. fault) in time stepping schemes; corrected bug in Update[].

0.81: Generalization of transformation jacobians (spherical and rectangular,
with optional parameters); changed handling of missing command line arguments; 
enhanced Print OnCut; fixed memory leak for time domain analysis of coupled 
problems; -name option; fixed seg. fault in ILUK.

0.80: Fixed computation of time derivatives on first time step (in 
post-processing); added tolerance in transformation jacobians; fixed parsing of 
DOS files (carriage return problems); automatic memory reallocation in 
ILUD/ILUK.

0.79: Various bug fixes (mainly for the post-processing of intergal quantities); 
avtomatic treatment of degenerated cases in axisymmetrical problems.

0.78: Various bug fixes.

0.77: Changed syntax for PostOperations (Plot suppressed in favour of Print; 
Plot OnRegion becomes Print OnElementsOf); changed table oriented 
post-processing formats; new binary formats; new error diagnostics.

0.76: Reorganized high order shape functions; optimization of the 
post-processing (faster and less bloated); lots of internal cleanups.

0.74: High order shape functions; lots of small bug fixes.

0.73: Eigen value problems (Lanczos); minor corrections.

0.7: constraint syntax; fourier transform; unary minus correction; complex 
integral quantity correction; separate iteration matrix generation.

0.6: Second order time derivatives; Newton nonlinear scheme; Newmark time 
stepping scheme; global quantity syntax; interactive post-processing; tensors; 
integral quantities; post-processing facilities.

0.3: First distributed version.
Appendix G Copyright and credits

GetDP is copyright (C) 1997-2020

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and

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University of Liege

Major code contributions to GetDP have been provided by Johan Gyselinck, Ruth Sabariego, Michael Asam and Bertrand Thierry. Other code contributors include: David Colignon, Tuan Ledinh, Patrick Lefevre, Andre Nicolet, Jean-Francois Remacle, Timo Tarhasaari, Christophe Trophime and Marc Ume. See the source code for more details.

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